

Sequence Modeling: Generation



CS 288: Advanced Natural Language Processing

Generation

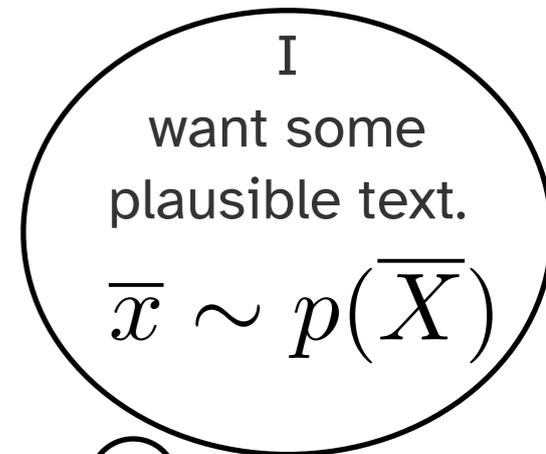


- Given a language model $p(\bar{X}) \in \Delta^{\mathcal{V}^+}$, how do we get a plausible sequence out of it?

- Autoregressive language model:

$$p(\bar{x}) = \prod_{i=1}^n p(x_i \mid x_1, \dots, x_{i-1})$$

- We can sample directly from this approximation
- We can adjust this distribution, then sample from it
- We can try to find the *most* plausible sequence in \mathcal{V}^+



Sequential Generation



$$p(\bar{x}) = \prod_{i=1}^n p(x_i \mid x_1, \dots, x_{i-1})$$

- As we generate, we build our output sequence \bar{x} , which starts as an empty sequence $\bar{x} = \langle \rangle$

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- At each step i , we choose an item from the vocabulary \mathcal{V} by performing some operation on the local probability distribution $p(X_i \mid x_1, \dots, x_{i-1}) \in \Delta^{\mathcal{V}}$

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- Then, we append this to our running sequence $\bar{x} \leftarrow \bar{x} + \langle x_i \rangle$

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- Then, we append this to our running sequence $\bar{x} \leftarrow \bar{x} + \langle x_i \rangle$
- If we ever choose EOS, we stop generation
- **Main point:** generation methods differ wrt the **operation** they perform on $p(X_i \mid x_1, \dots, x_{i-1})$

Recap: Ancestral Sampling



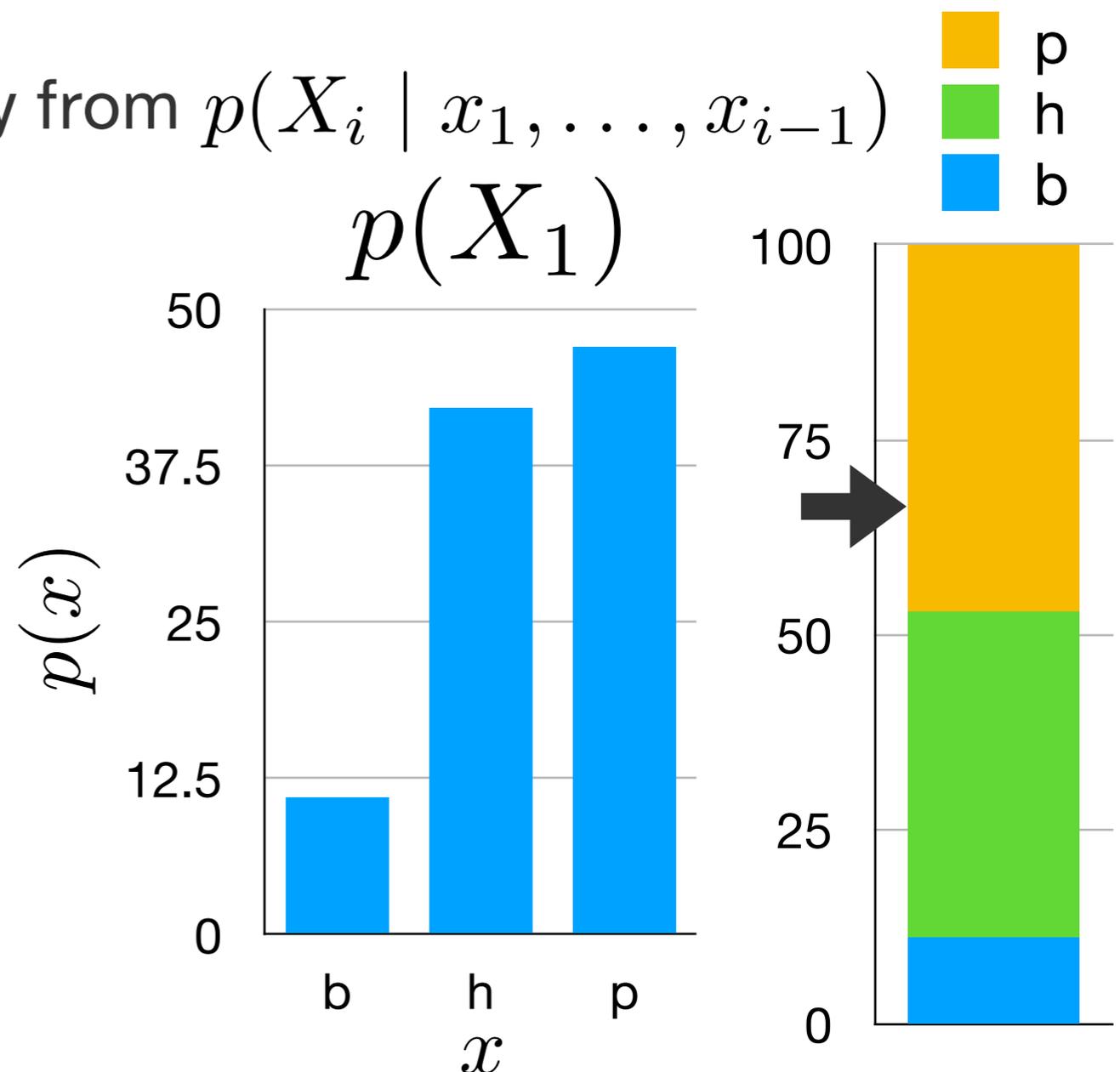
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Operation: sample directly from $p(X_i \mid x_1, \dots, x_{i-1})$

$$\bar{x} = \langle p \rangle$$

`number = random(0, 100)`

number is 65



Recap: Ancestral Sampling



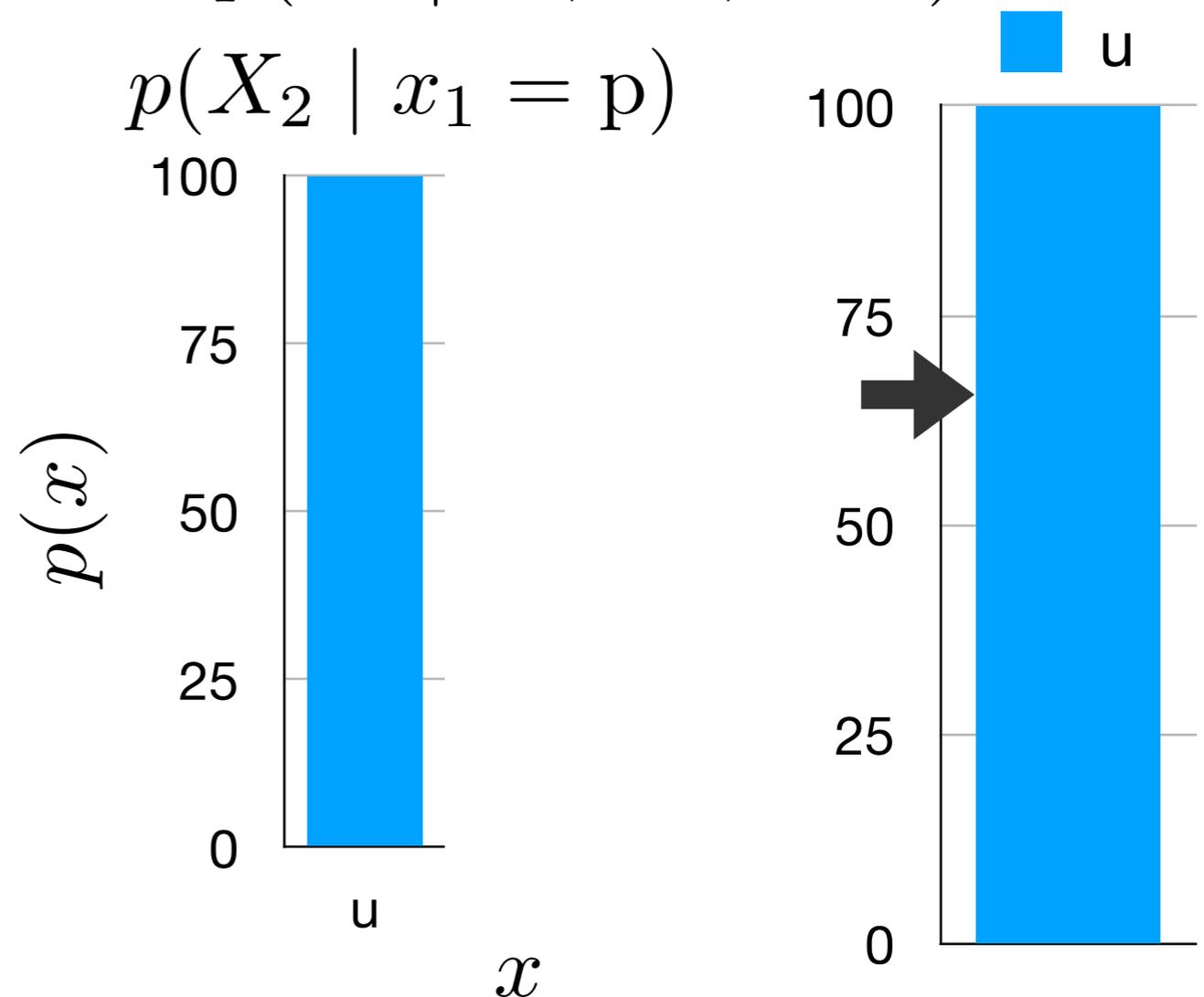
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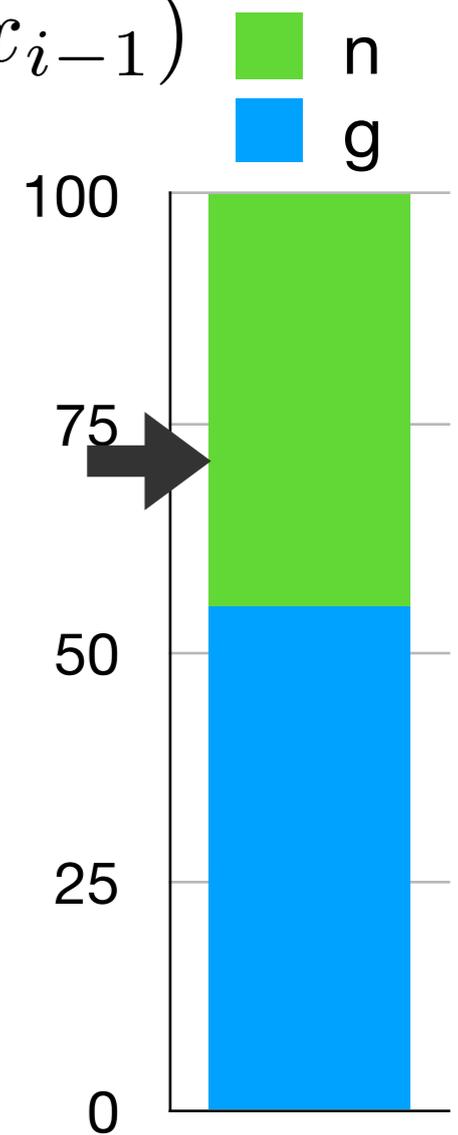
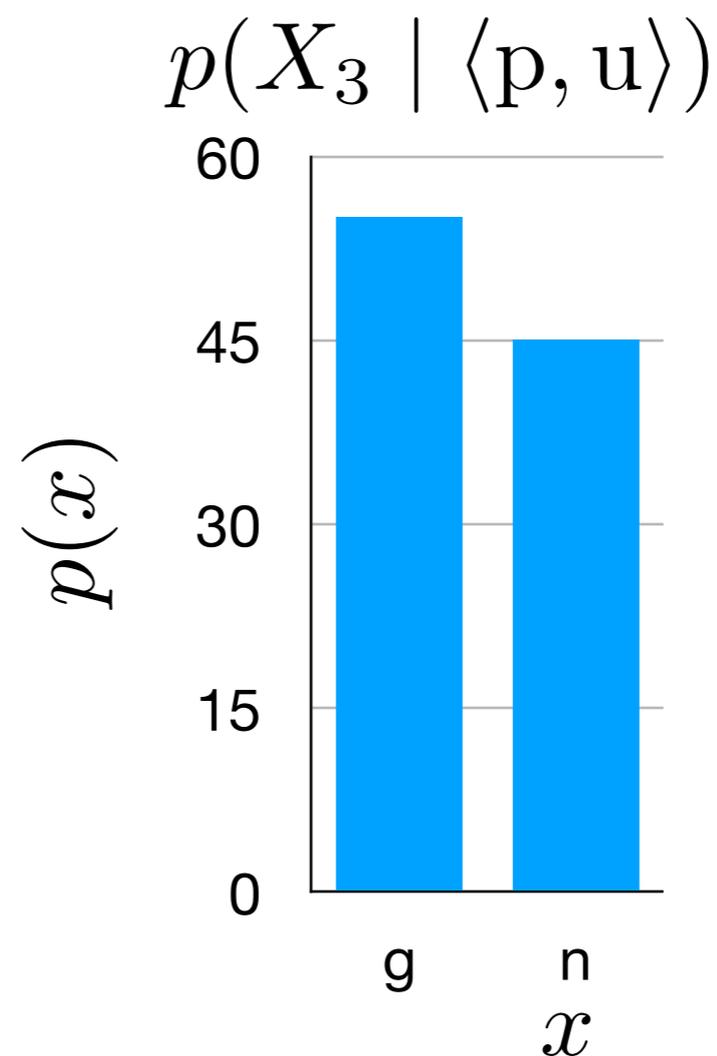
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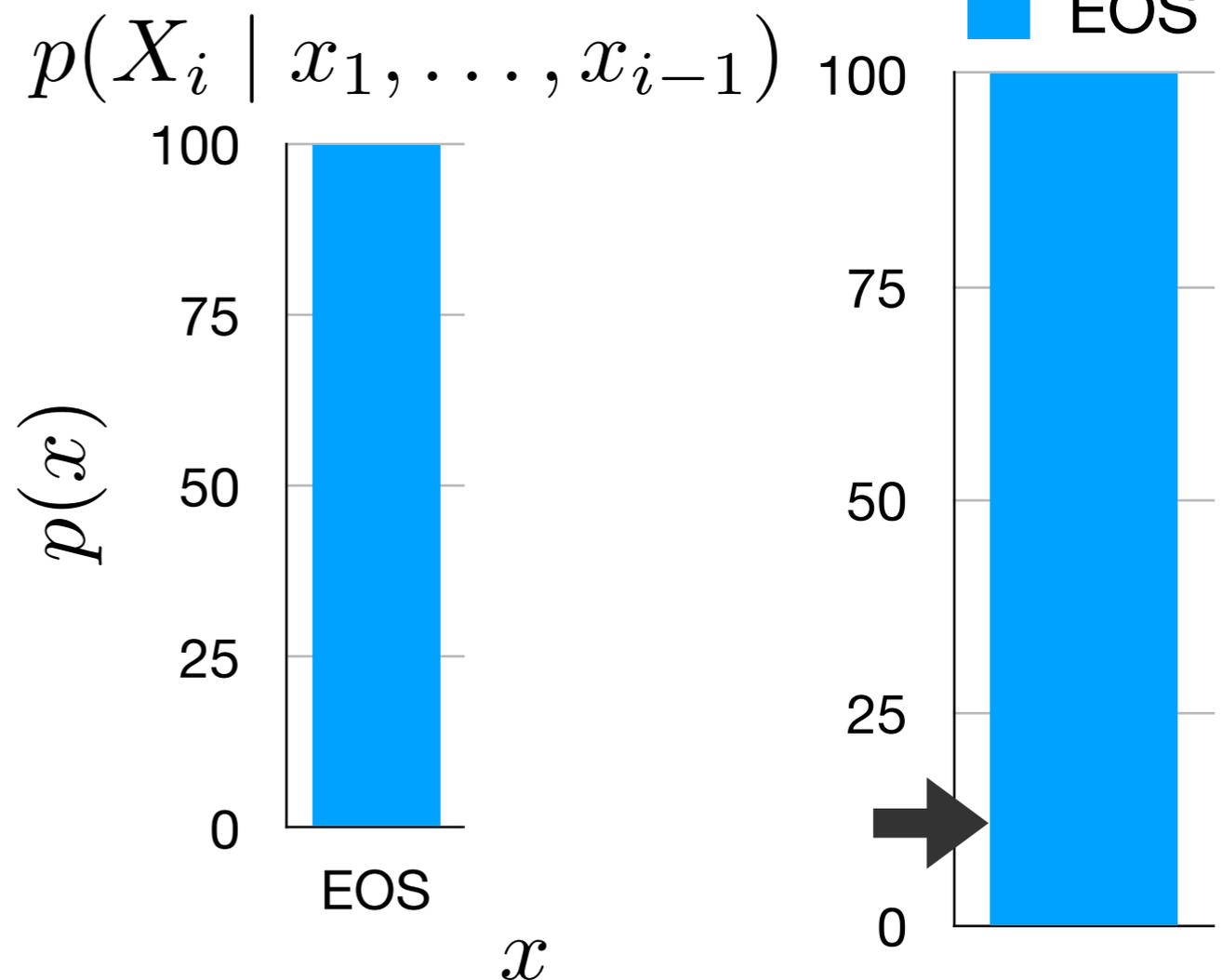
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$$\bar{x} = \left\langle \begin{array}{l} p \text{ } u \text{ } n \text{ EOS} \\ p \text{ } u \text{ } n \end{array} \right\rangle$$



Adjusting the Temperature



Operation: modify the logits
before computing probabilities



Sneak peek: computing probabilities over wordtypes using pretty much any modern language model

- Score each wordtype independently

$$s(w) = f(w \mid x_1, \dots, x_{i-1}; \theta) \quad \leftarrow \text{logits}$$

- Renormalize using softmax

$$p(X_i = w \mid x_1, \dots, x_{i-1}) = \frac{\exp(s(w))}{\sum_{w' \in \mathcal{V}} \exp(s(w'))}$$

Adjusting the Temperature



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**Temperature parameter controls the
“smoothness” of this distribution:**

$$p(X_i = w \mid x_1, \dots, x_{i-1}) = \frac{\exp(s(w)/\tau)}{\sum_{w' \in \mathcal{V}} \exp(s(w')/\tau)}$$

Adjusting the Temperature

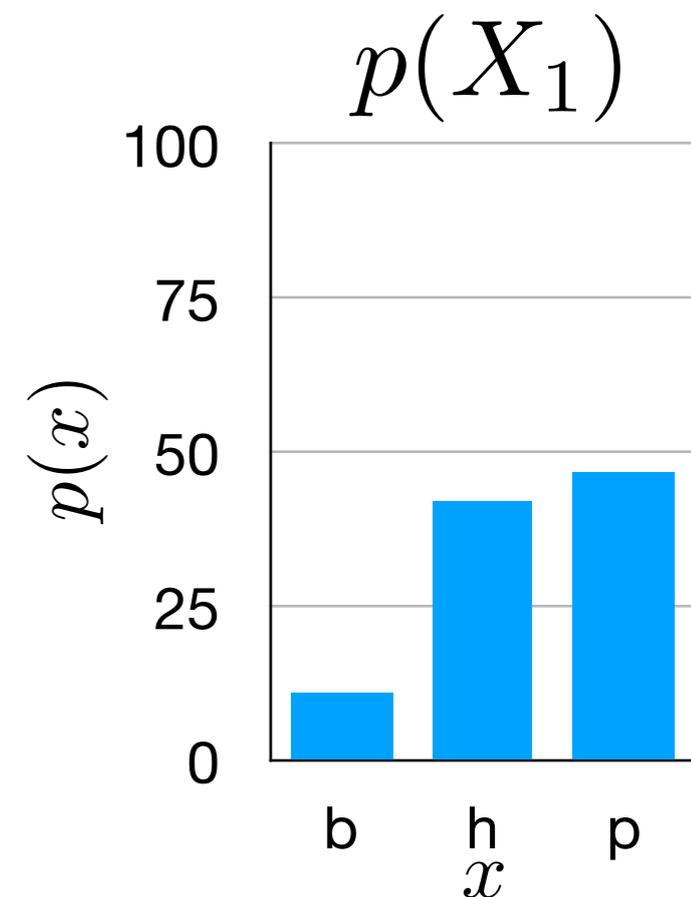


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- $\tau = 1$: no changes to the probability distribution



Adjusting the Temperature

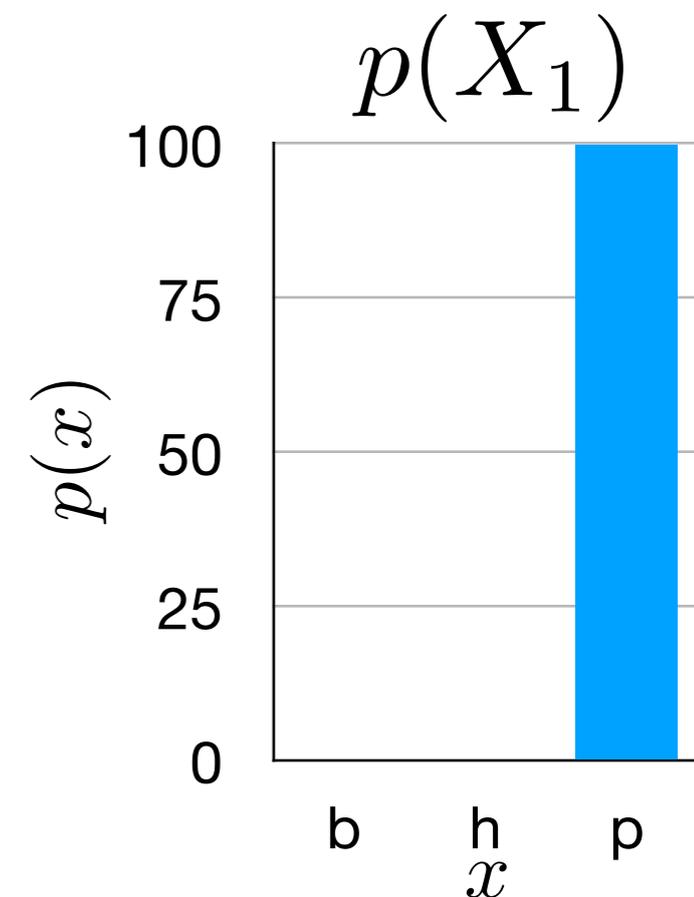


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- $\tau = 1$: no changes to the probability distribution
- $\tau \rightarrow 0$: relative probability assigned to highest-probability item in distribution increases
 - in practice, setting a temperature of 0 recovers “argmax”, putting all of the mass on the highest-probability item



Adjusting the Temperature

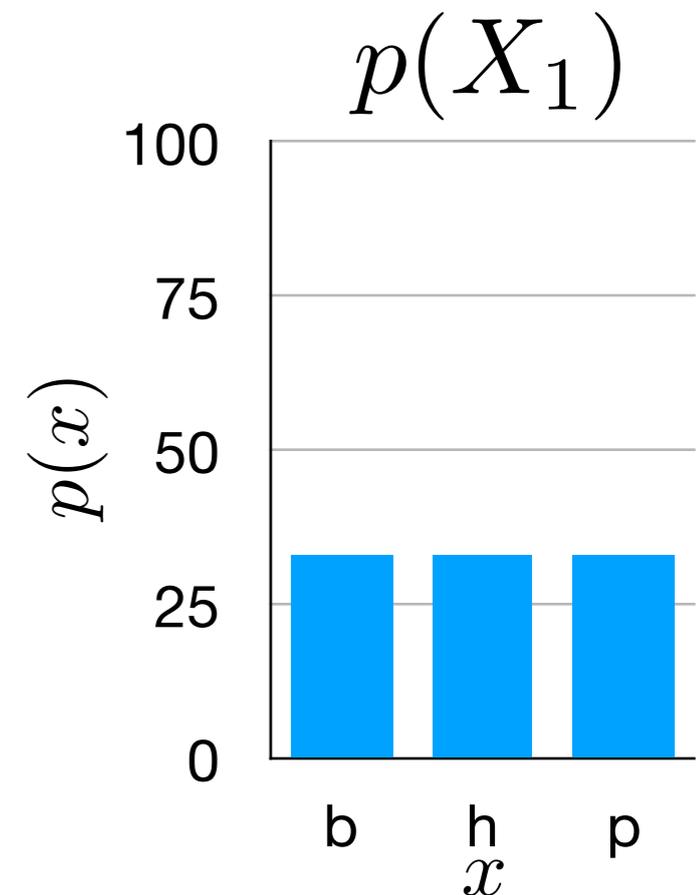


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- $\tau = 1$: no changes to the probability distribution
- $\tau \rightarrow 0$: relative probability assigned to highest-probability item in distribution increases
- $\tau \rightarrow \infty$: distribution becomes more and more uniform



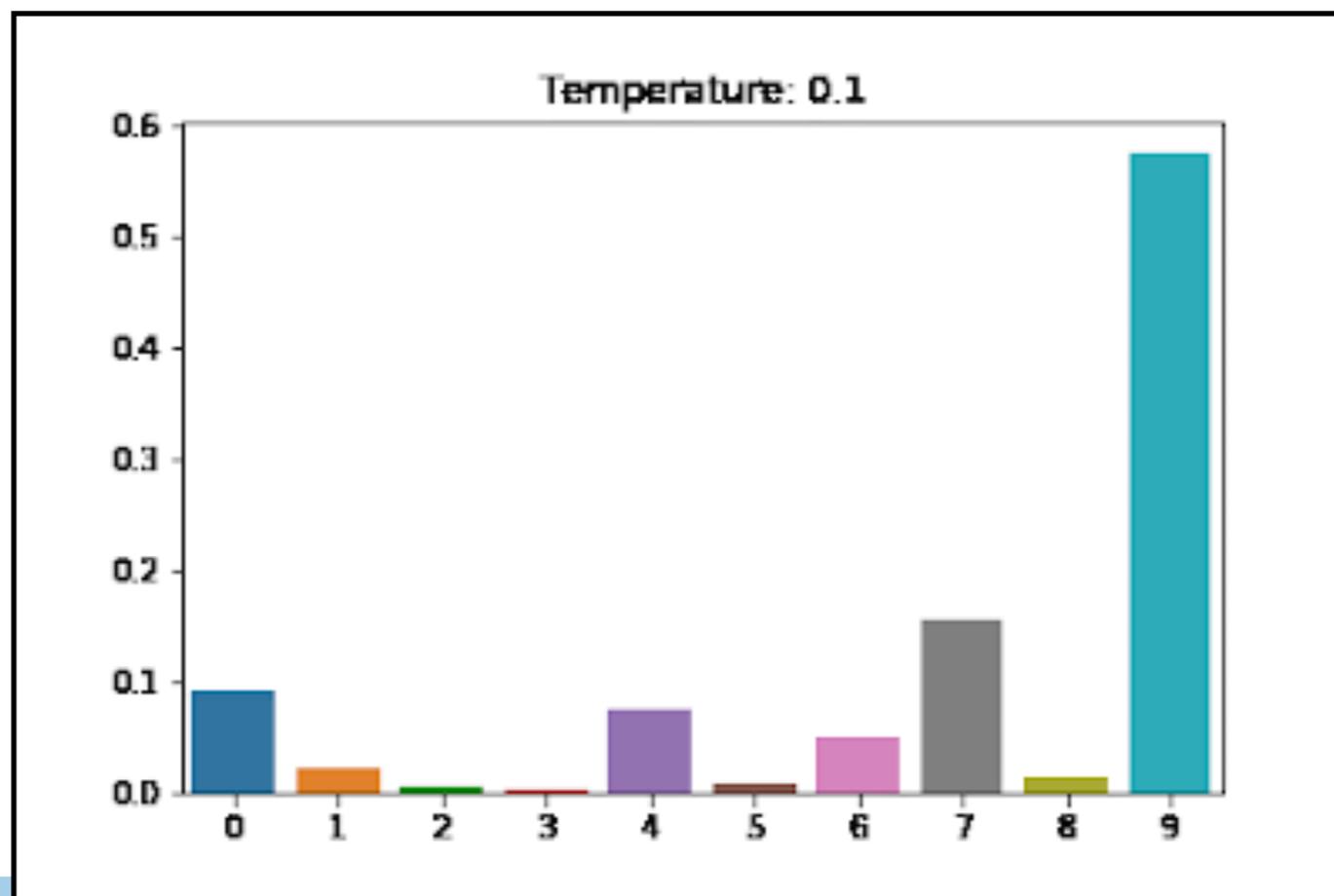
Adjusting the Temperature



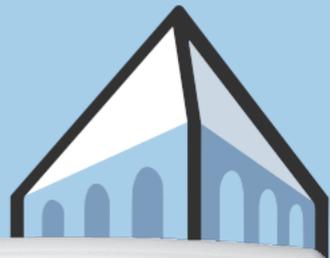
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Adjusting the Temperature



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Temp = 0	Temp = 5																																																				
Once upon a time, there was a little	Once upon a time, there was a young																																																				
<table><tr><td>little</td><td>100%</td></tr><tr><td>beautiful</td><td>0%</td></tr><tr><td>young</td><td>0%</td></tr><tr><td>girl</td><td>0%</td></tr><tr><td>small</td><td>0%</td></tr><tr><td>king</td><td>0%</td></tr><tr><td>man</td><td>0%</td></tr><tr><td>kingdom</td><td>0%</td></tr><tr><td>very</td><td>0%</td></tr><tr><td>boy</td><td>0%</td></tr><tr><td>princess</td><td>0%</td></tr><tr><td>great</td><td>0%</td></tr><tr><td>⋮</td><td></td></tr></table>	little	100%	beautiful	0%	young	0%	girl	0%	small	0%	king	0%	man	0%	kingdom	0%	very	0%	boy	0%	princess	0%	great	0%	⋮		<table><tr><td>little</td><td>6%</td></tr><tr><td>beautiful</td><td>6%</td></tr><tr><td>young</td><td>6%</td></tr><tr><td>girl</td><td>5%</td></tr><tr><td>small</td><td>5%</td></tr><tr><td>king</td><td>5%</td></tr><tr><td>man</td><td>5%</td></tr><tr><td>kingdom</td><td>5%</td></tr><tr><td>very</td><td>4%</td></tr><tr><td>boy</td><td>4%</td></tr><tr><td>princess</td><td>4%</td></tr><tr><td>great</td><td>4%</td></tr><tr><td>⋮</td><td></td></tr></table>	little	6%	beautiful	6%	young	6%	girl	5%	small	5%	king	5%	man	5%	kingdom	5%	very	4%	boy	4%	princess	4%	great	4%	⋮	
little	100%																																																				
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- **Temperature allows us to control the entropy of the output distribution without changing its relative ranking of items**
- Higher temperature: closer to a uniform distribution
- Lower temperature: “peakier” distribution (in the limit, gives all probability mass to the most probable item)

Finding the Most Probable Sequence



Operation: find $\arg \max_{\bar{x} \in \mathcal{V}^+} p(\bar{x})$

- Why is this hard?

Finding the Most Probable Sequence



Operation: find $\arg \max_{\bar{x} \in \mathcal{V}^+} p(\bar{x})$

- Why is this hard?
- An approximation: greedy “sampling”

$$x_i \leftarrow \arg \max_{x \in \mathcal{V}} p(X_i \mid x_1, \dots, x_{i-1})$$

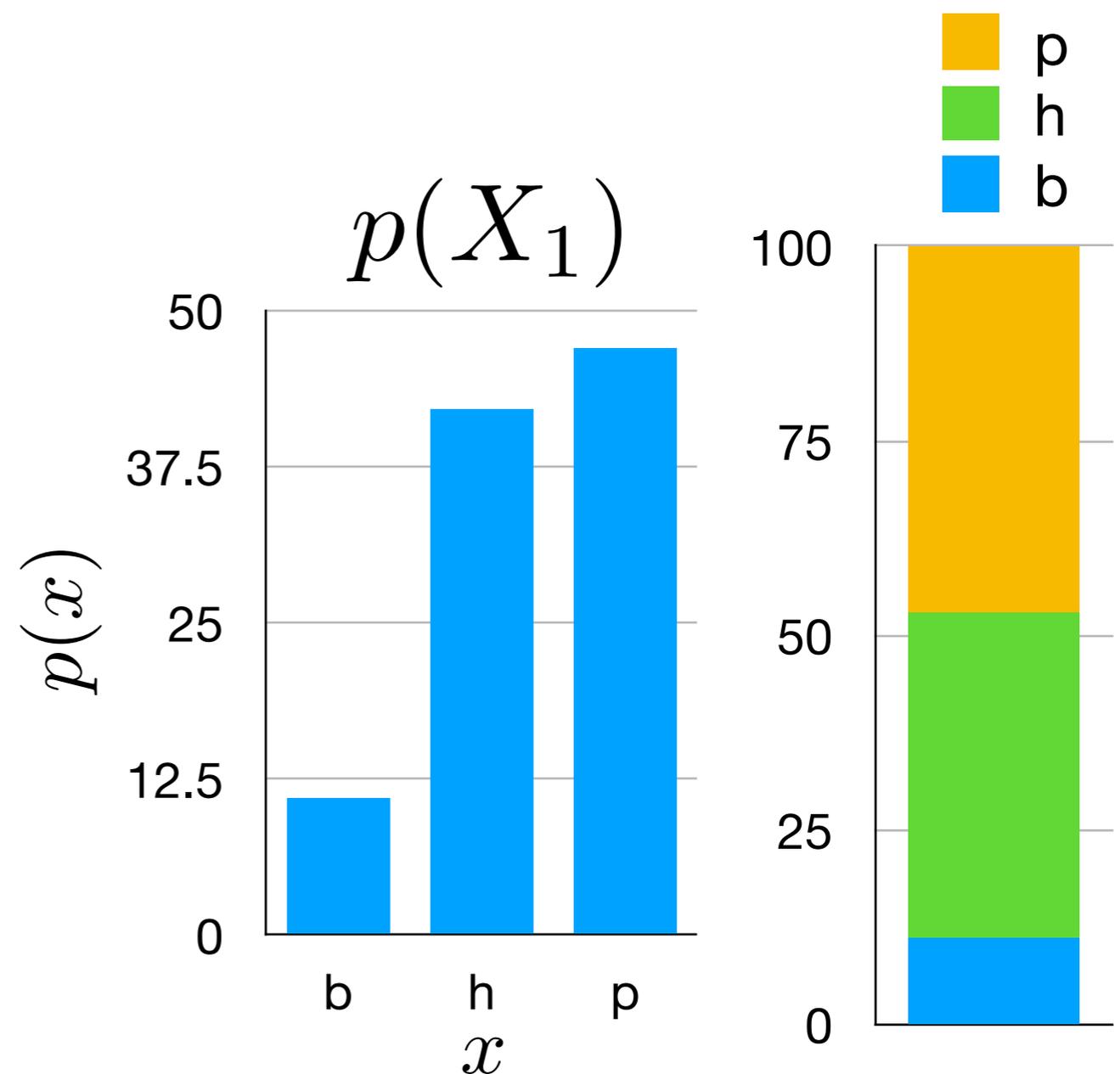
- Just choose the most probable wordtype at each generation step (no random sampling needed)

Finding the Most Probable Sequence



Operation: choose $x_i \leftarrow \arg \max_{x \in \mathcal{V}} p(X_i | x_1, \dots, x_{i-1})$

$$\overline{x} = \langle p \rangle$$

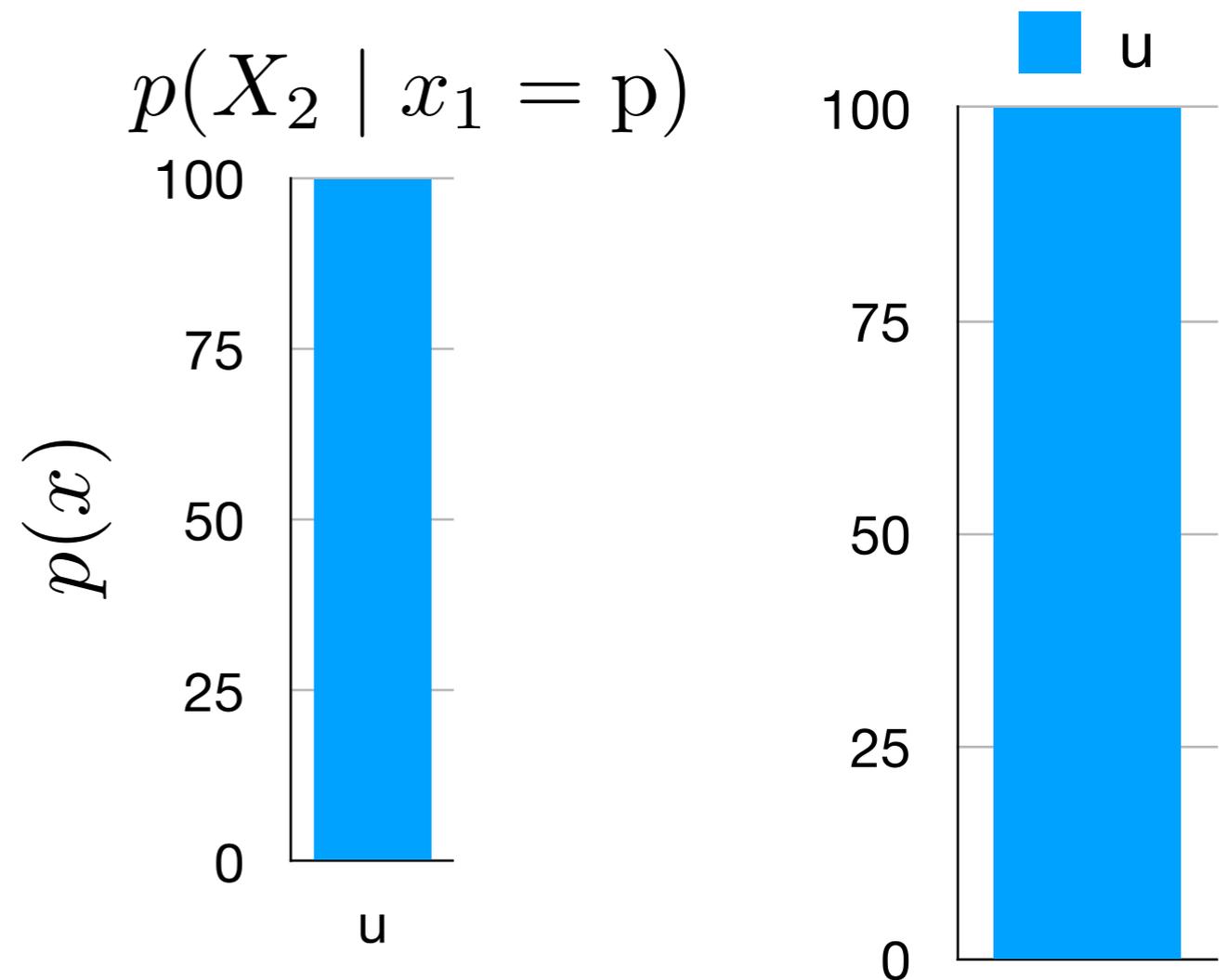


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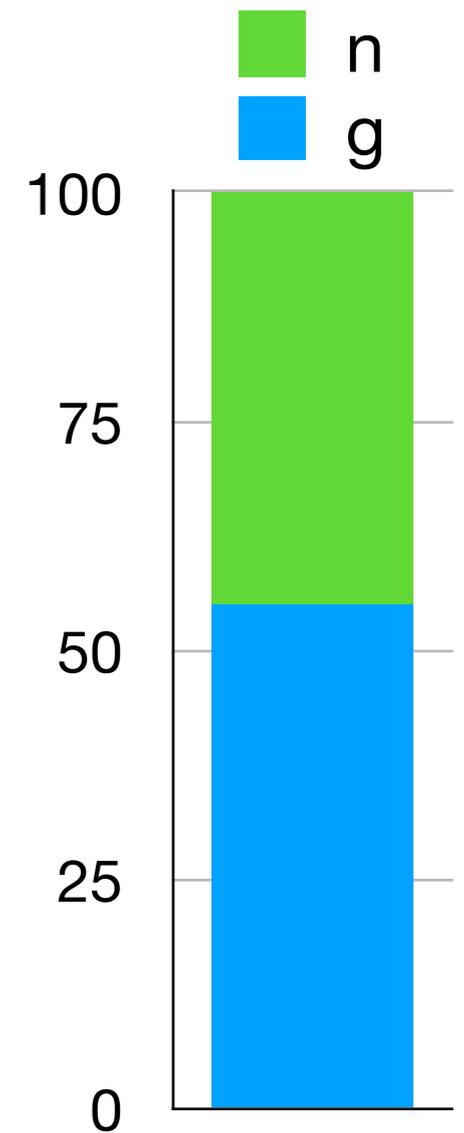
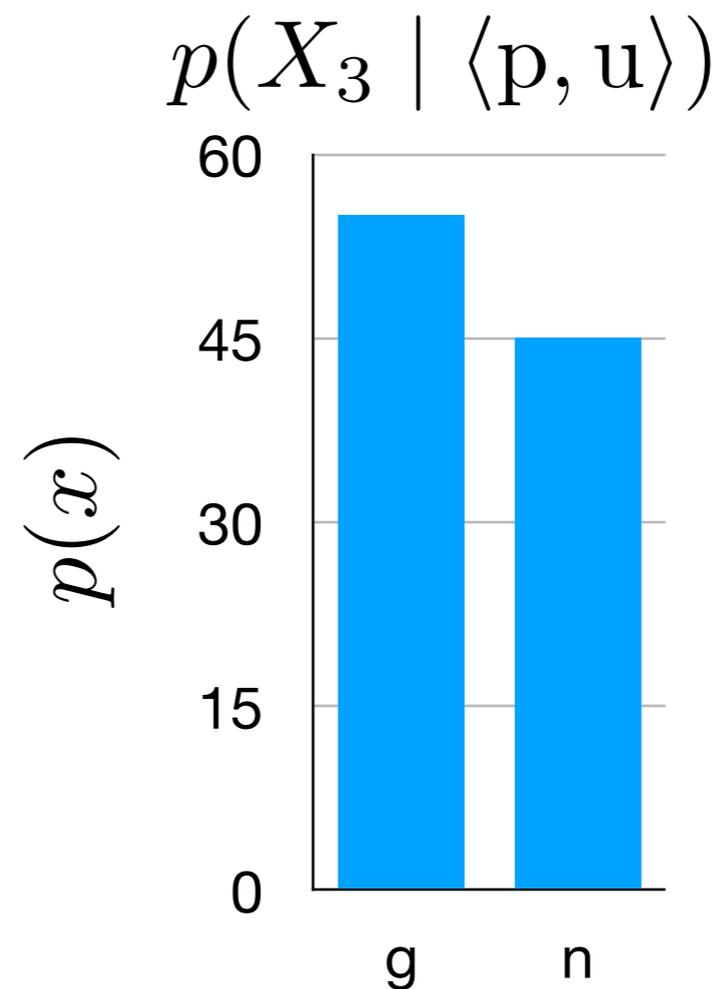


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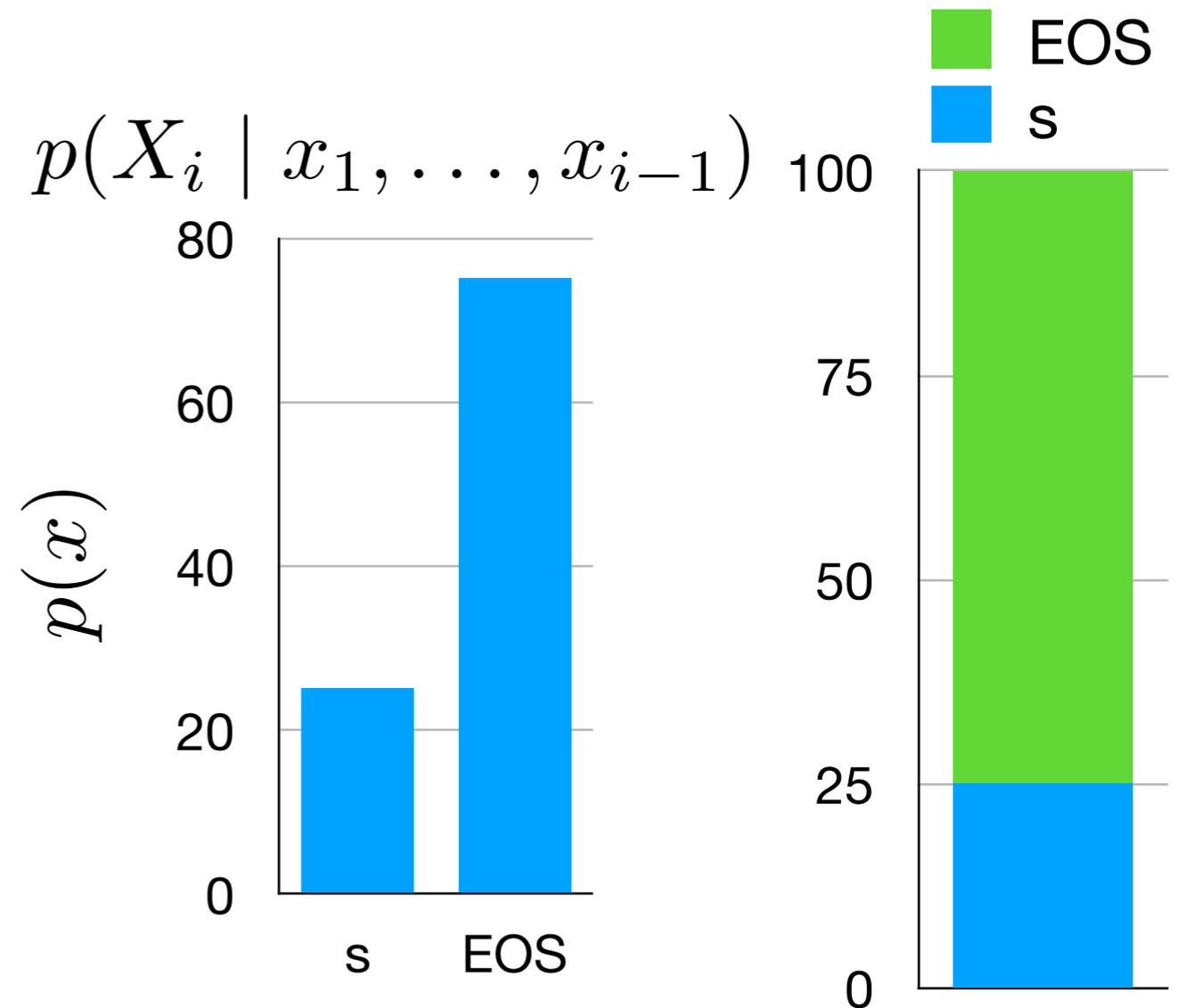
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Operation: choose $x_i \leftarrow \arg \max_{x \in \mathcal{V}} p(X_i | x_1, \dots, x_{i-1})$

$$\overline{x} = \langle pug_{\text{EOS}} \rangle$$

pug



Finding the Most Probable Sequence



Operation: choose $x_i \leftarrow \arg \max_{x \in \mathcal{V}} p(X_i \mid x_1, \dots, x_{i-1})$

- Why isn't this guaranteed to get us the highest-probability sequence?
- A better approximation for global argmax: **beam search**
 - During generation, we maintain a “beam” of n sequences instead of just one
 - At each generation step i ,

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 - Then we look at all the n^2 sequences so far, and discard all but the n most likely sequences
 - At the end, we select the sequence that has the highest probability among the set

Beam Search, $n = 3$



$p(X_1)$

the



0.4

in



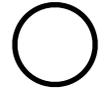
0.3

and



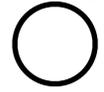
0.2

every



0.1

way



0.1

Beam Search, $n = 3$



$p(X_1)$

the



0.4

in



0.3

and



0.2

Discard all but the top 3 continuations

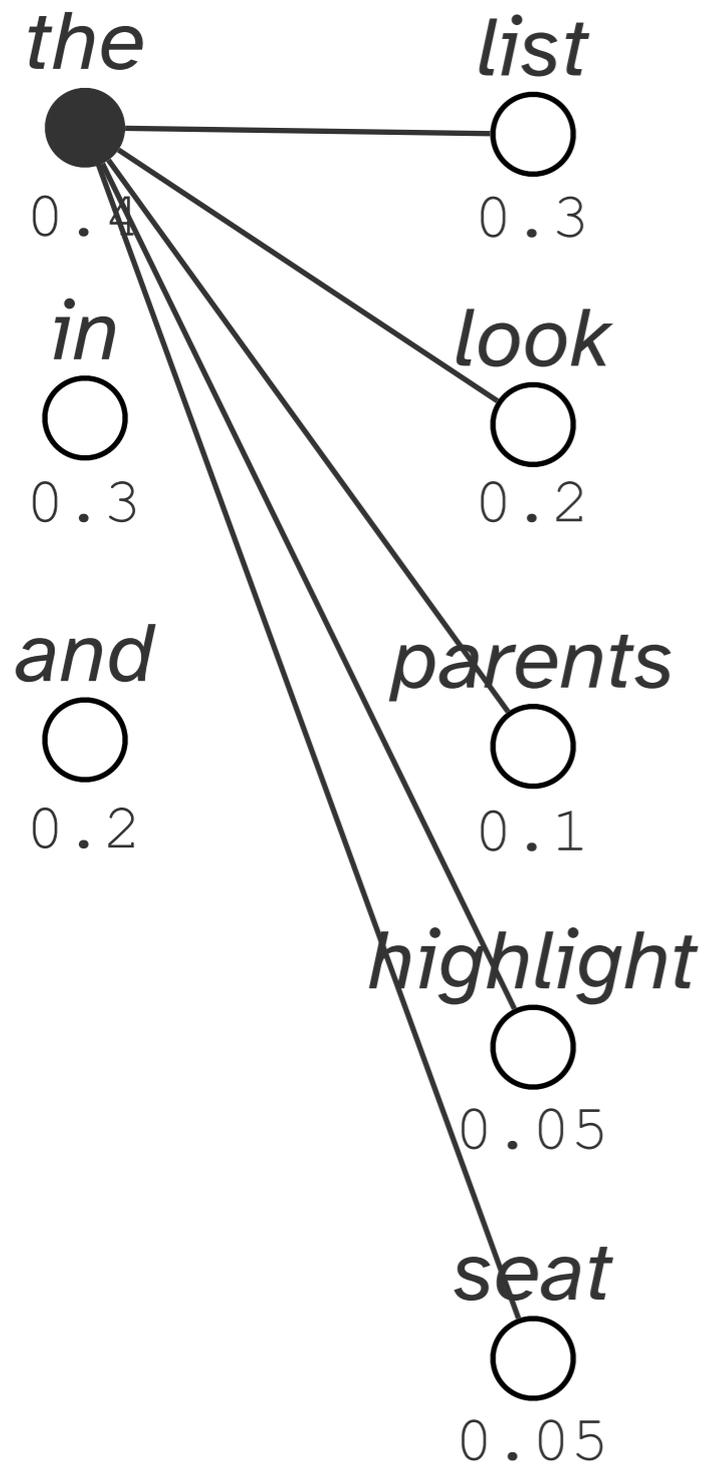
Beam

	Prefix	Probability
	the	0.4
	in	0.3
	and	0.2

Beam Search, $n = 3$



$$p(X_1) \quad p(X_2 \mid x_1 = \text{the})$$



Continue with beam item #1 as prefix

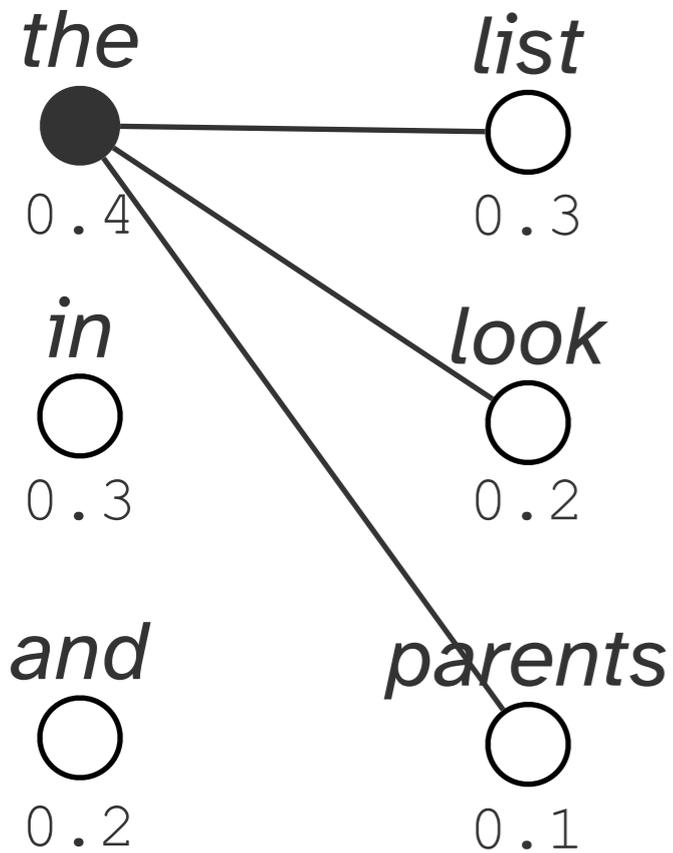
Beam

Prefix	Probability
the	0.04
in	0.02
and	0.02

Beam Search, $n = 3$



$$p(X_1) \quad p(X_2 \mid x_1 = \text{the})$$



Discard all but the top 3 continuations

Current Beam Candidates

Prefix	Probability
the list	$0.4 * 0.3$
the look	$0.3 * 0.2$
the parents	$0.2 * 0.1$

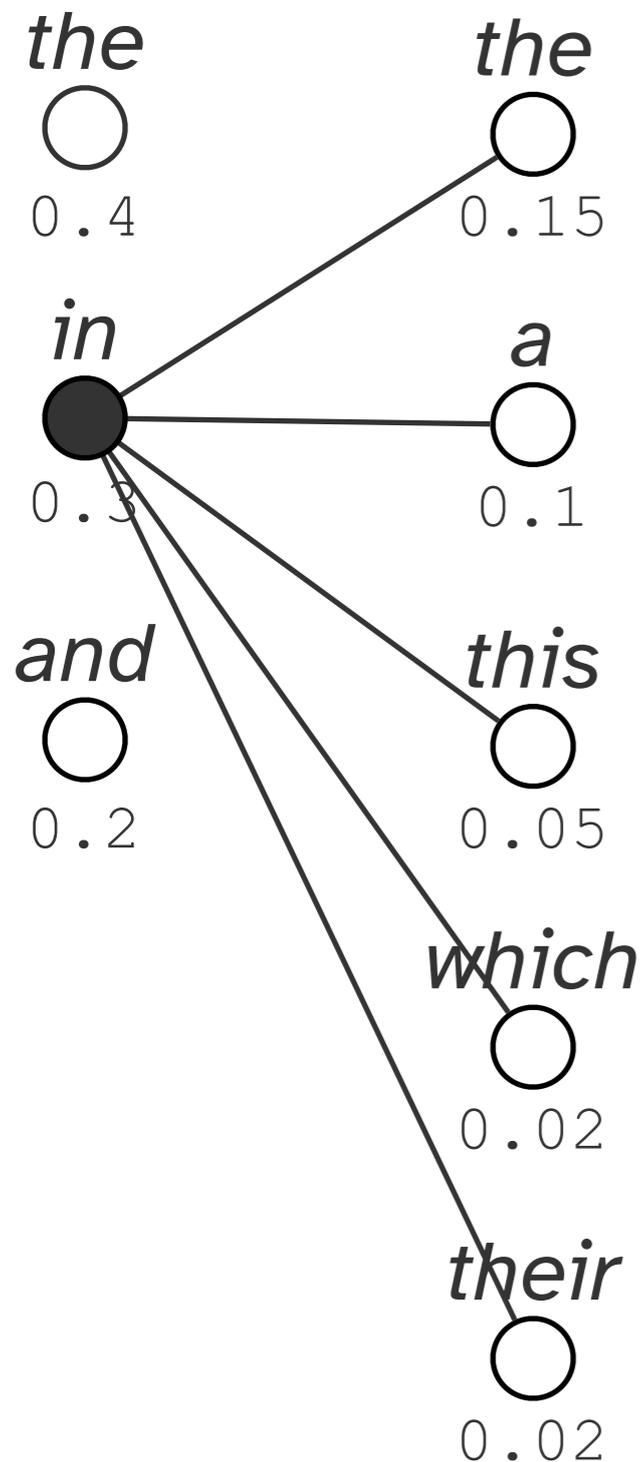
Beam

Prefix	Probability
the	0.04
in	0.02
and	0.02

Beam Search, $n = 3$



$$p(X_1)p(X_2 | x_1 = \text{in})$$



Continue with beam item #2 as prefix

Current Beam Candidates

Prefix	Probability
the list	$0.4 * 0.3$
the look	$0.3 * 0.2$
the parents	$0.2 * 0.1$

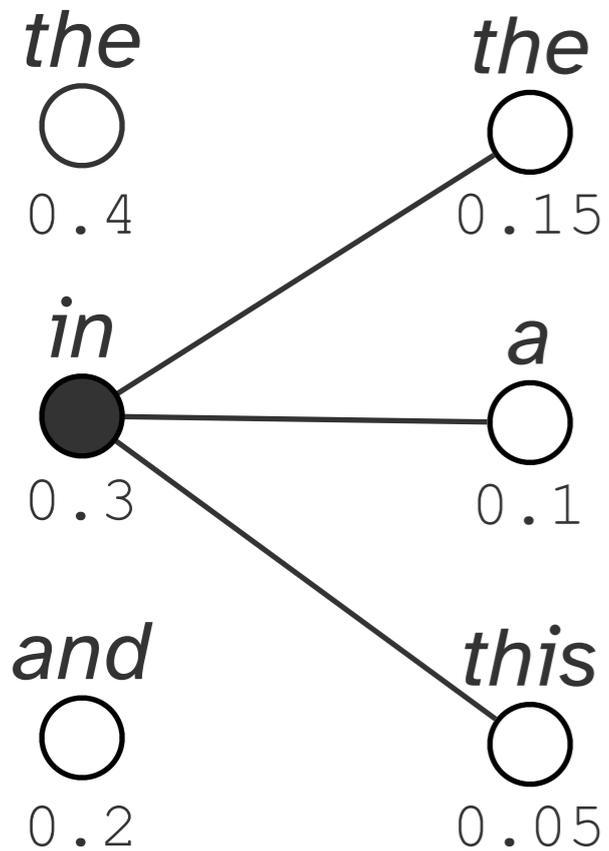
Beam

Prefix	Probability
the	0.04
in	0.02
and	0.02

Beam Search, $n = 3$



$$p(X_1)p(X_2 | x_1 = \text{in})$$



Discard all but the top 3 continuations

Current Beam Candidates

Prefix	Probability
the list	$0.4 * 0.3$
the look	$0.3 * 0.2$
the parents	$0.2 * 0.1$
in the	$0.3 * 0.15$
in a	$0.3 * 0.1$
in this	$0.3 * 0.05$

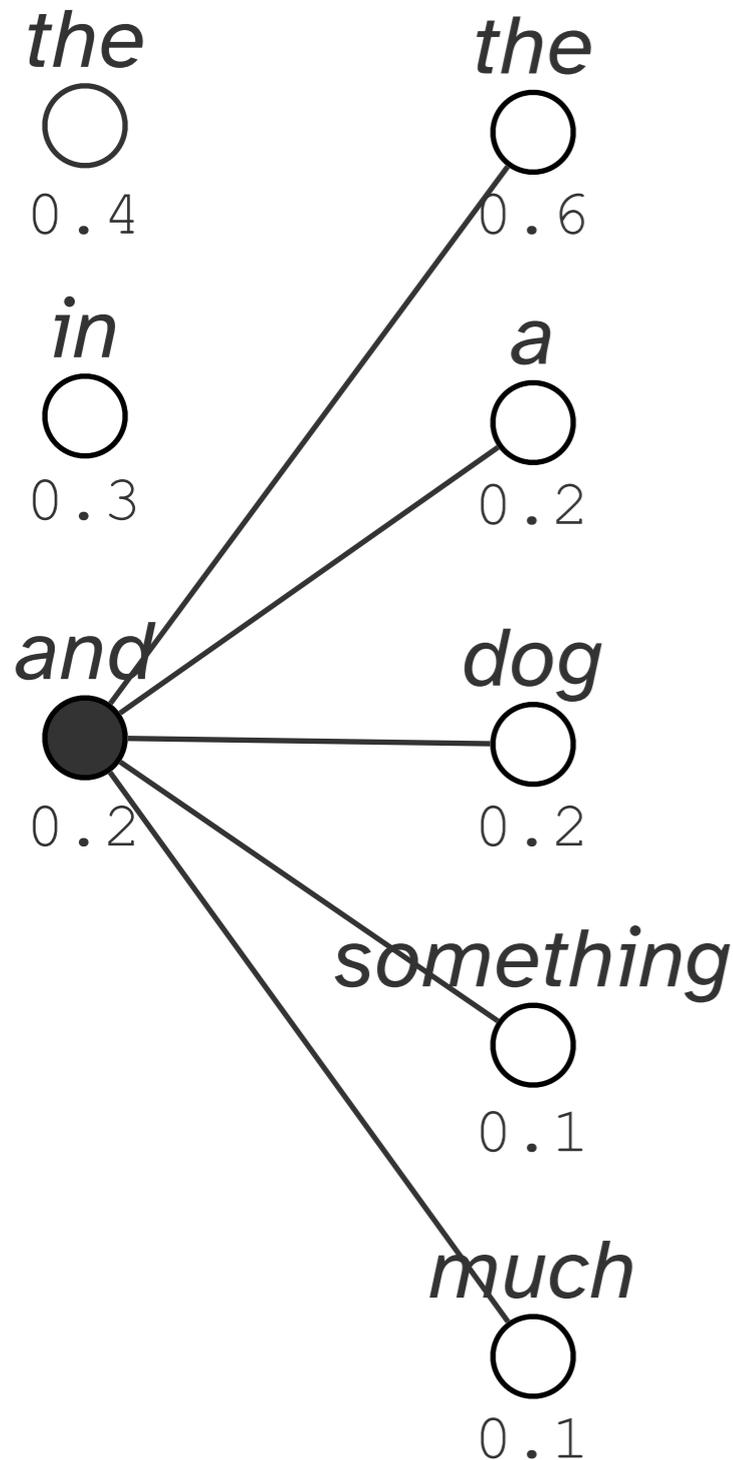
Beam

Prefix	Probability
the	0.04
in	0.02
and	0.02

Beam Search, $n = 3$



$$p(X_1) p(X_2 | x_1 = \text{and})$$



Continue with beam item #3 as prefix

Current Beam Candidates

Prefix	Probability
the list	$0.4 * 0.3$
the look	$0.3 * 0.2$
the parents	$0.2 * 0.1$
in the	$0.3 * 0.15$
in a	$0.3 * 0.1$
in this	$0.3 * 0.05$

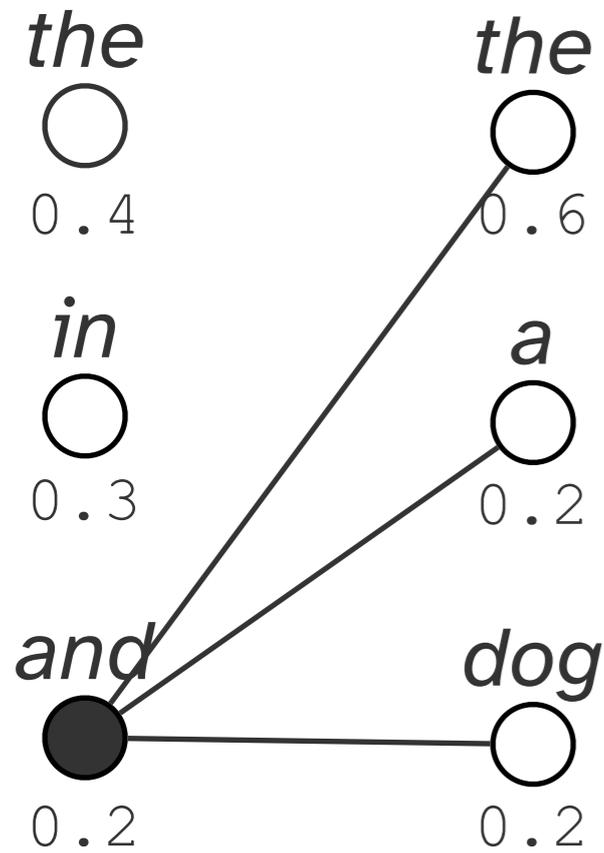
Beam

Prefix	Probability
the	0.04
in	0.02
and	0.02

Beam Search, $n = 3$



$$p(X_1) p(X_2 | x_1 = \text{and})$$



Discard all but the top 3 continuations

Current Beam Candidates

Prefix	Probability
the list	$0.4 * 0.3$
the look	$0.3 * 0.2$
the parents	$0.2 * 0.1$
in the	$0.3 * 0.15$
in a	$0.3 * 0.1$
in this	$0.3 * 0.05$
and the	$0.2 * 0.6$
and a	$0.2 * 0.2$
and dog	$0.2 * 0.2$

Beam

Prefix	Probability
the	0.04
in	0.02
and	0.02

Beam Search, $n = 3$



Compute probabilities
of all candidates

**Current Beam
Candidates**

Prefix	Probability
the list	0.12
the look	0.06
the parents	0.02
in the	0.05
in a	0.03
in this	0.02
and the	0.12
and a	0.04
and dog	0.04

Beam

Prefix	Probability
the	0.04
in	0.02
and	0.02

Beam Search, $n = 3$



Refresh the beam
with top n candidates

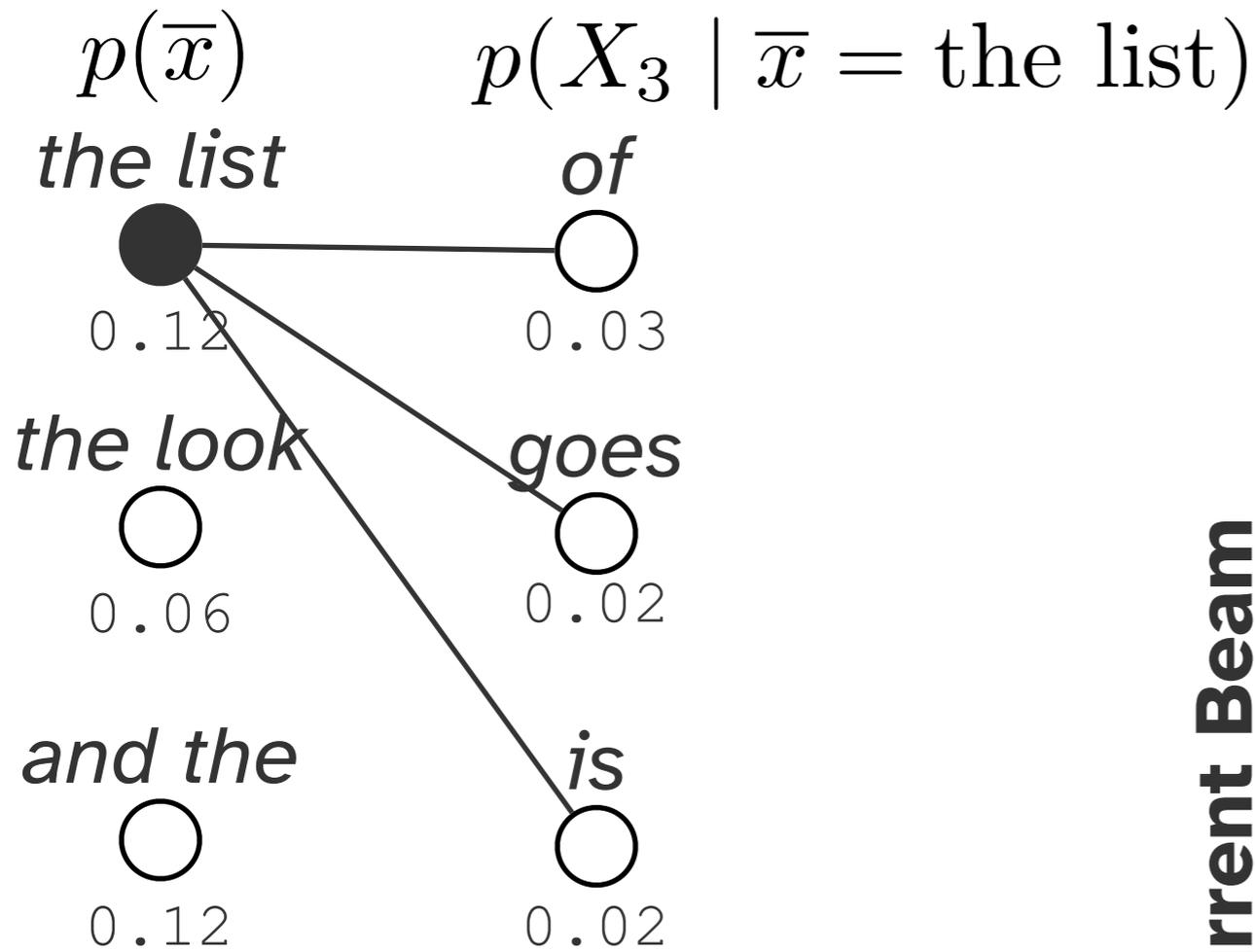
Current Beam
Candidates

Prefix	Probability
the list	0.12
the look	0.06
the parents	0.02
in the	0.05
in a	0.03
in this	0.02
and the	0.12
and a	0.04
and dog	0.04

Beam

Prefix	Probability
the list	0.12
the look	0.06
and the	0.12

Beam Search, $n = 3$



Keep generating
with new beam

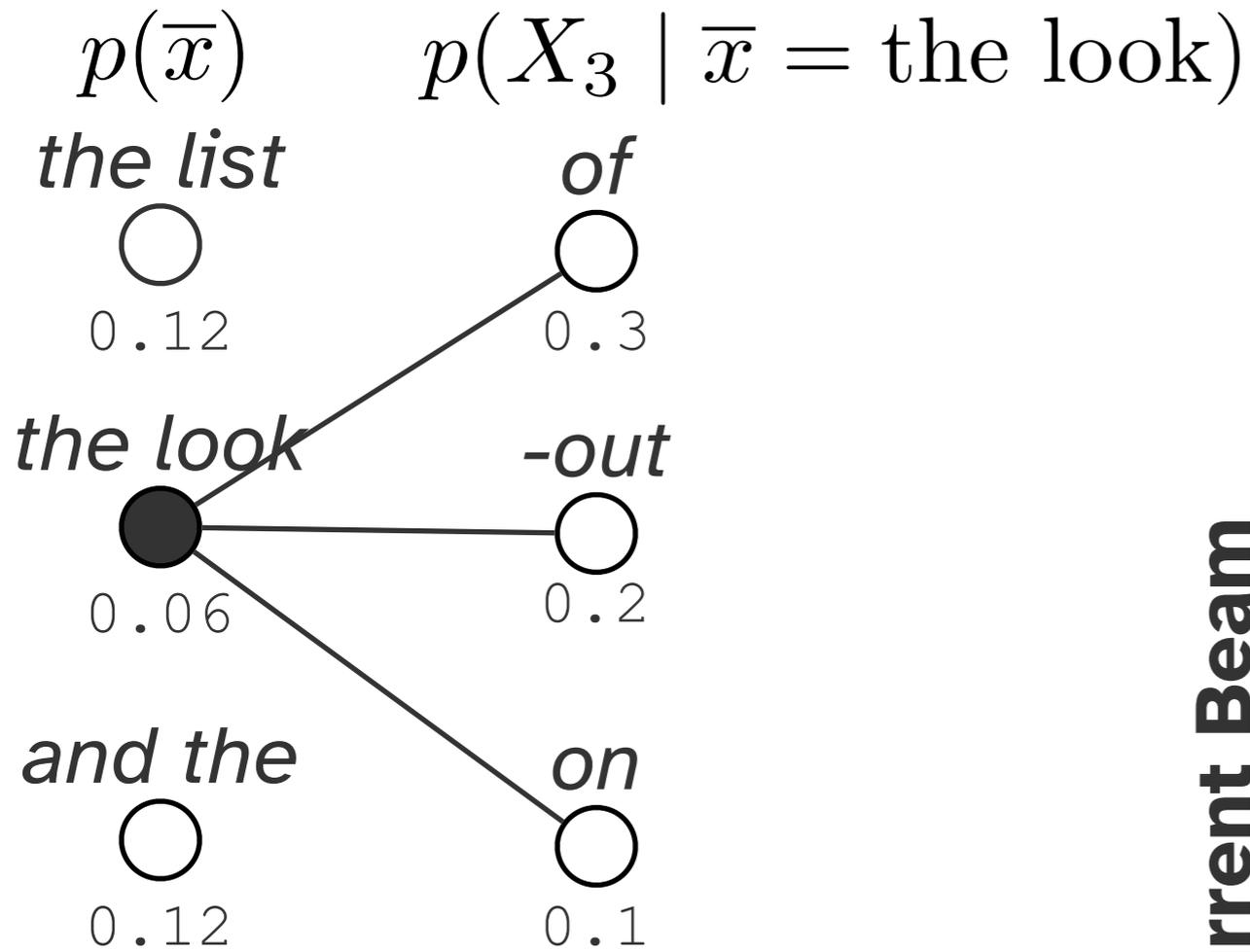
Current Beam Candidates

Prefix	Probability
the list of	0.004
the list goes	0.002
the list is	0.002

Beam

Prefix	Probability
the list	0.12
the look	0.06
and the	0.12

Beam Search, $n = 3$



Keep generating with new beam

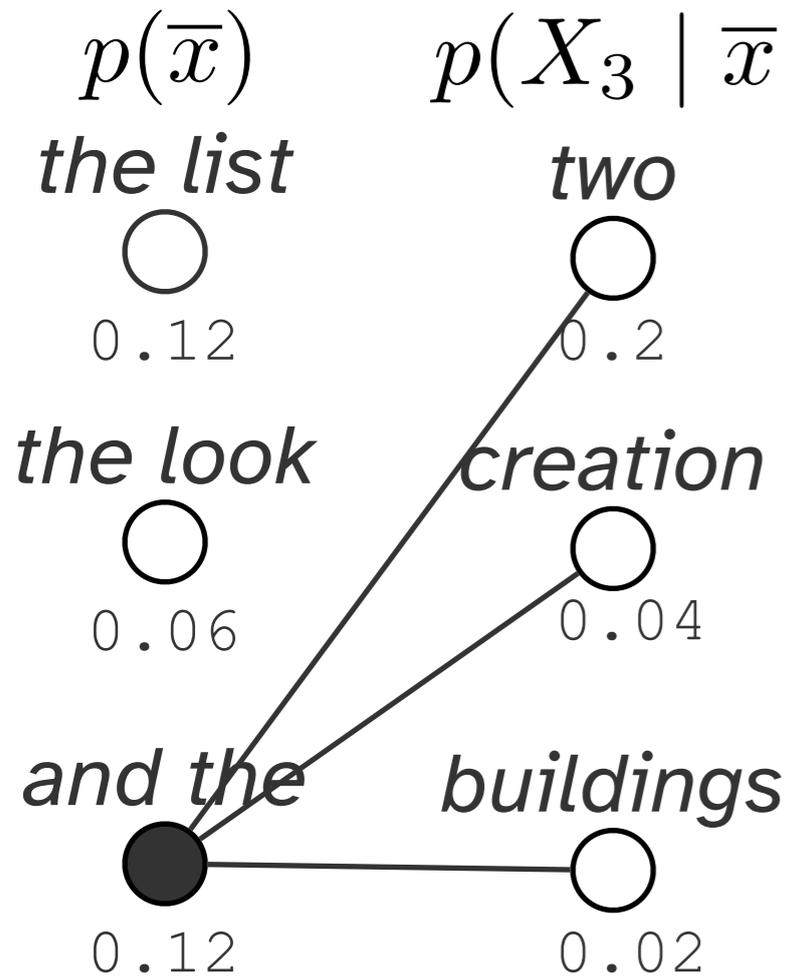
Current Beam Candidates

Prefix	Probability
the list of	0.004
the list goes	0.002
the list is	0.002
the look of	0.018
the lookout	0.012
the look on	0.006

Beam

Prefix	Probability
the list	0.12
the look	0.06
and the	0.12

Beam Search, $n = 3$



Keep generating with new beam

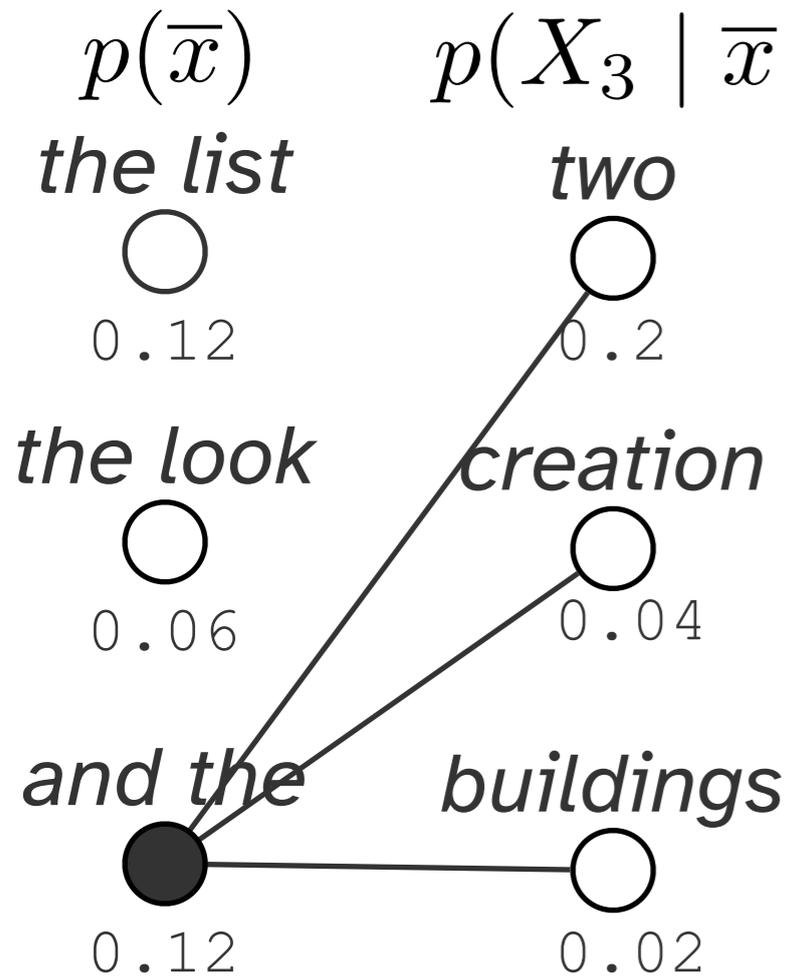
Current Beam Candidates

Prefix	Probability
the list of	0.004
the list goes	0.002
the list is	0.002
the look of	0.018
the lookout	0.012
the look on	0.006
and the two	0.024
and the creation	0.005
and the buildings	0.002

Beam

Prefix	Probability
the list	0.12
the look	0.06
and the	0.12

Beam Search, $n = 3$



Refresh the beam with top n candidates

Current Beam Candidates

Prefix	Probability
the list of	0.004
the list goes	0.002
the list is	0.002
the look of	0.018
the lookout	0.012
the look on	0.006
and the two	0.024
and the creation	0.005
and the buildings	0.002

Beam

Prefix	Probability
the look of	0.018
the lookout	0.012
and the two	0.024

Beam Search, $n = 3$



- How do we know when to stop?
 - When all of the items in the beam have EOS (we don't expand these prefixes, just keep them around for the end)
 - Or, when we've reached a maximum sequence length
- Let's say we're done sampling at this point
- We'll select the sequence with the highest probability in the beam

Beam

Prefix	Probability
the look of	0.018
the lookout	0.012
and the two	0.024

Beam Search, $n = 3$



- How do we know when to stop?
 - When all of the items in the beam have EOS (we don't expand these prefixes, just keep them around for the end)
 - Or, when we've reached a maximum sequence length
- Let's say we're done sampling at this point
- We'll select the sequence with the highest probability in the beam

Beam

Prefix	Probability
the look of	0.018
the lookout	0.012
and the two	0.024

Beam Search, $n = 3$



- How do we know when to stop?
 - When all of the items in the beam have EOS (we don't expand these prefixes, just keep them around for the end)
 - Or, when we've reached a maximum sequence length
- Let's say we're done sampling at this point
- We'll select the sequence with the highest probability in the beam
- What if our sequences have different lengths?

Length normalization:
$$p(\bar{x}) \propto -\frac{1}{|\bar{x}|^\alpha} \sum_{i=1}^{|\bar{x}|} \log p(x_i \mid x_1, \dots, x_{i-1})$$

Masking Out Wordtypes

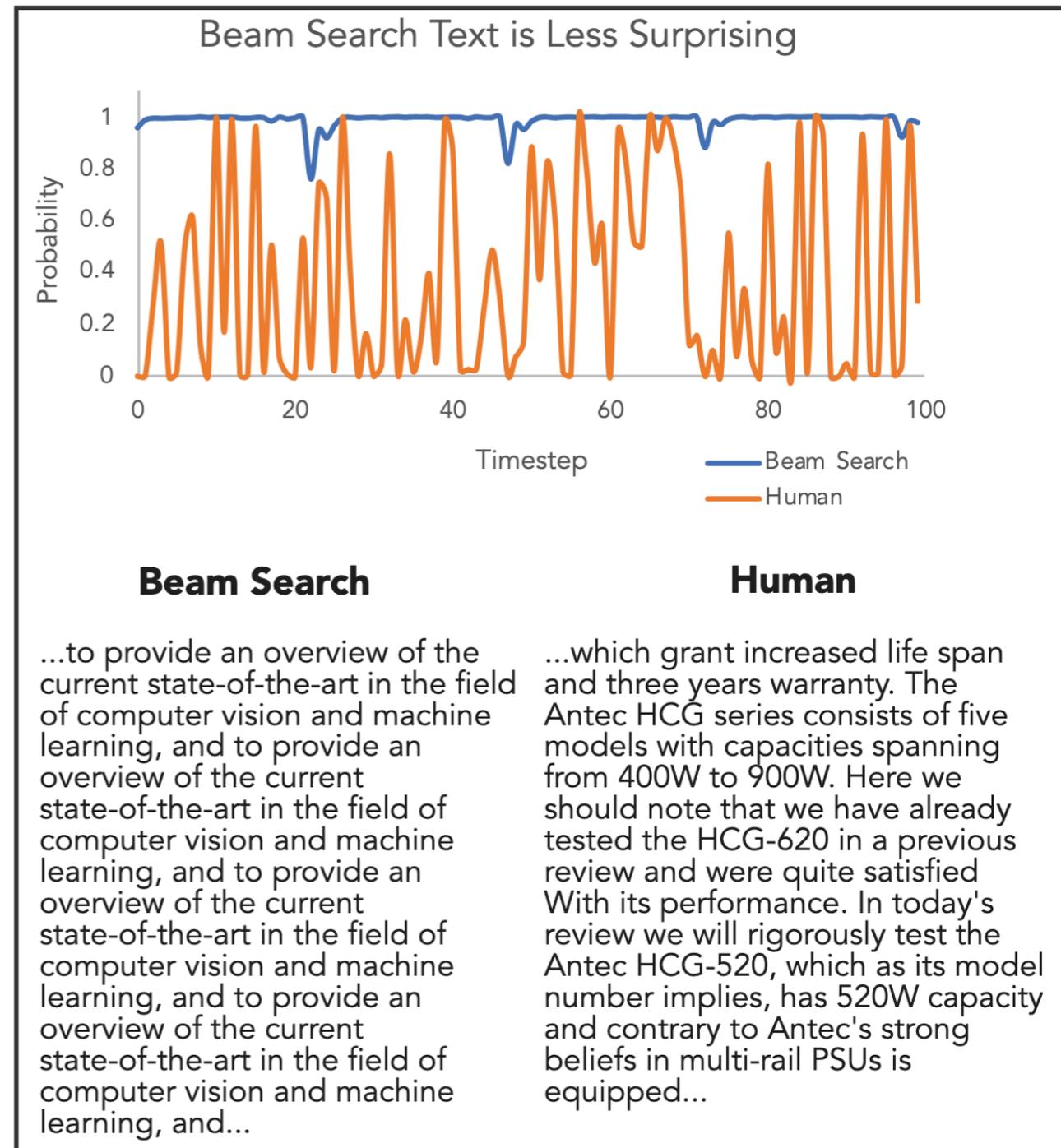


- Should we always try to approximate the argmax?

Masking Out Wordtypes



- Should we always try to approximate the argmax?
- Maybe not!
- Argmax produces repetitive, less diverse, and overall *too-probable* output sequences
- What's missing?

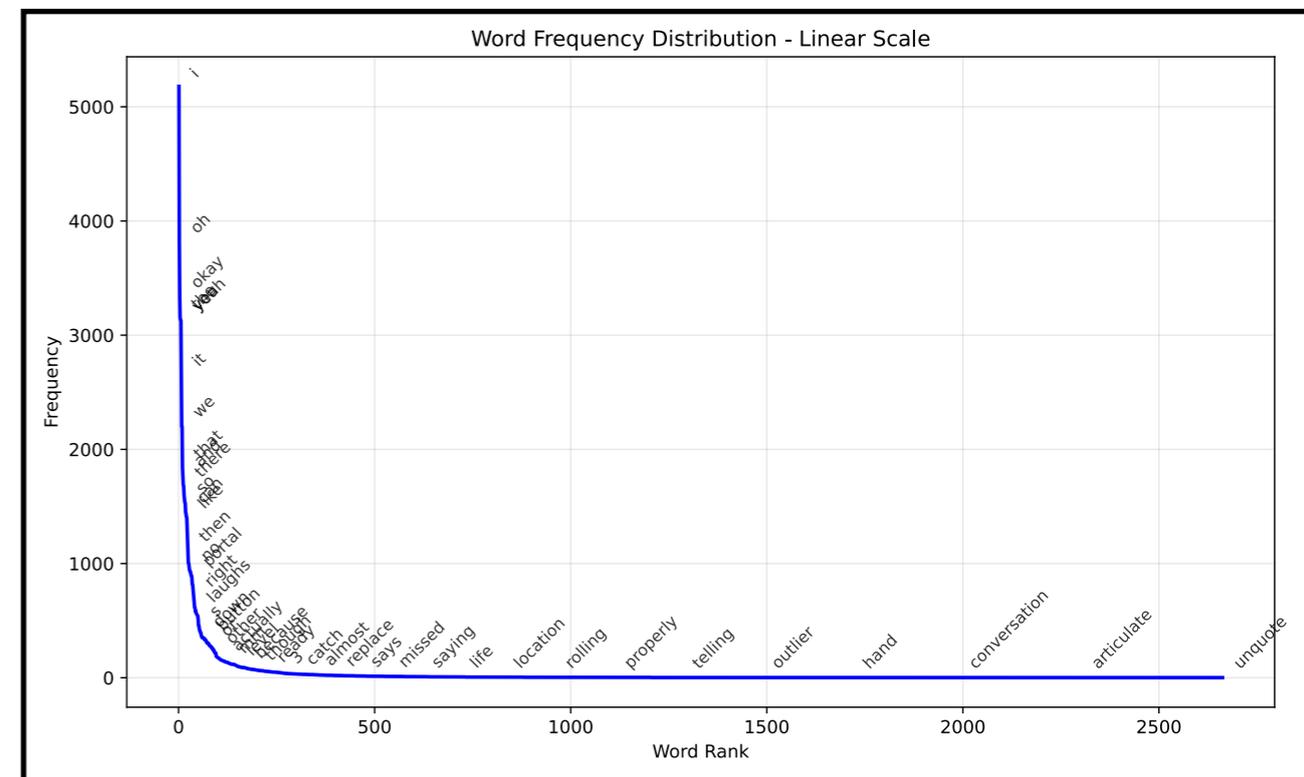


Holtzman et al. 2019

Masking Out Wordtypes



- Should we always try to approximate the argmax?
- Maybe not!
- Argmax produces repetitive, less diverse, and overall *too-probable* output sequences
- What's missing?
- Long tail!



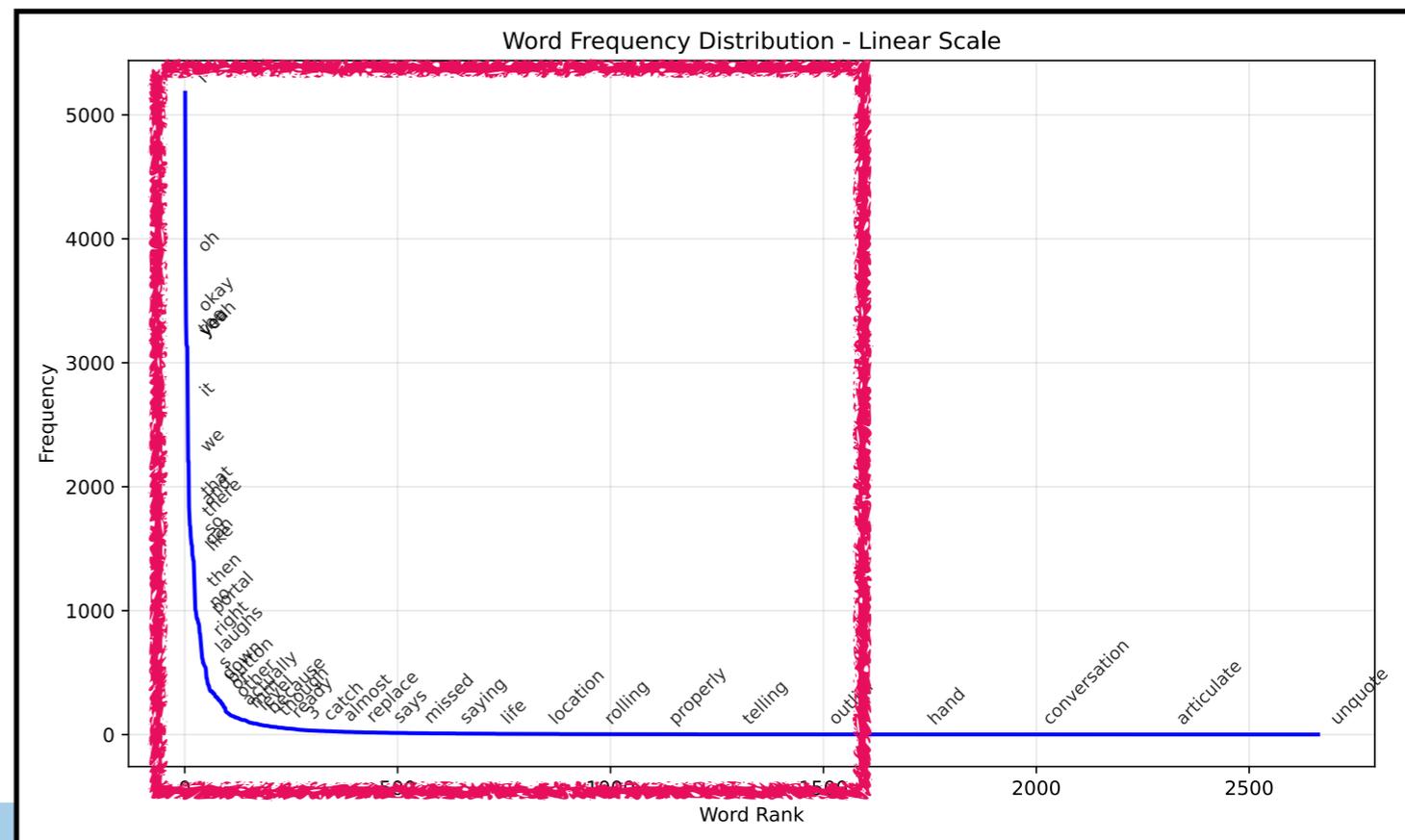
Masking Out Wordtypes



Operation: ϵ sampling

- Identify the set of n tokens \mathcal{E} such that $\forall x \in \mathcal{E}$,
 $p(x \mid x_1, \dots, x_{i-1}) \geq \epsilon$
- Set the probabilities of all but these tokens to 0
- Renormalize by dividing remaining probabilities by

$$\sum_{x \in \mathcal{E}} p(x \mid x_1, \dots, x_{i-1})$$



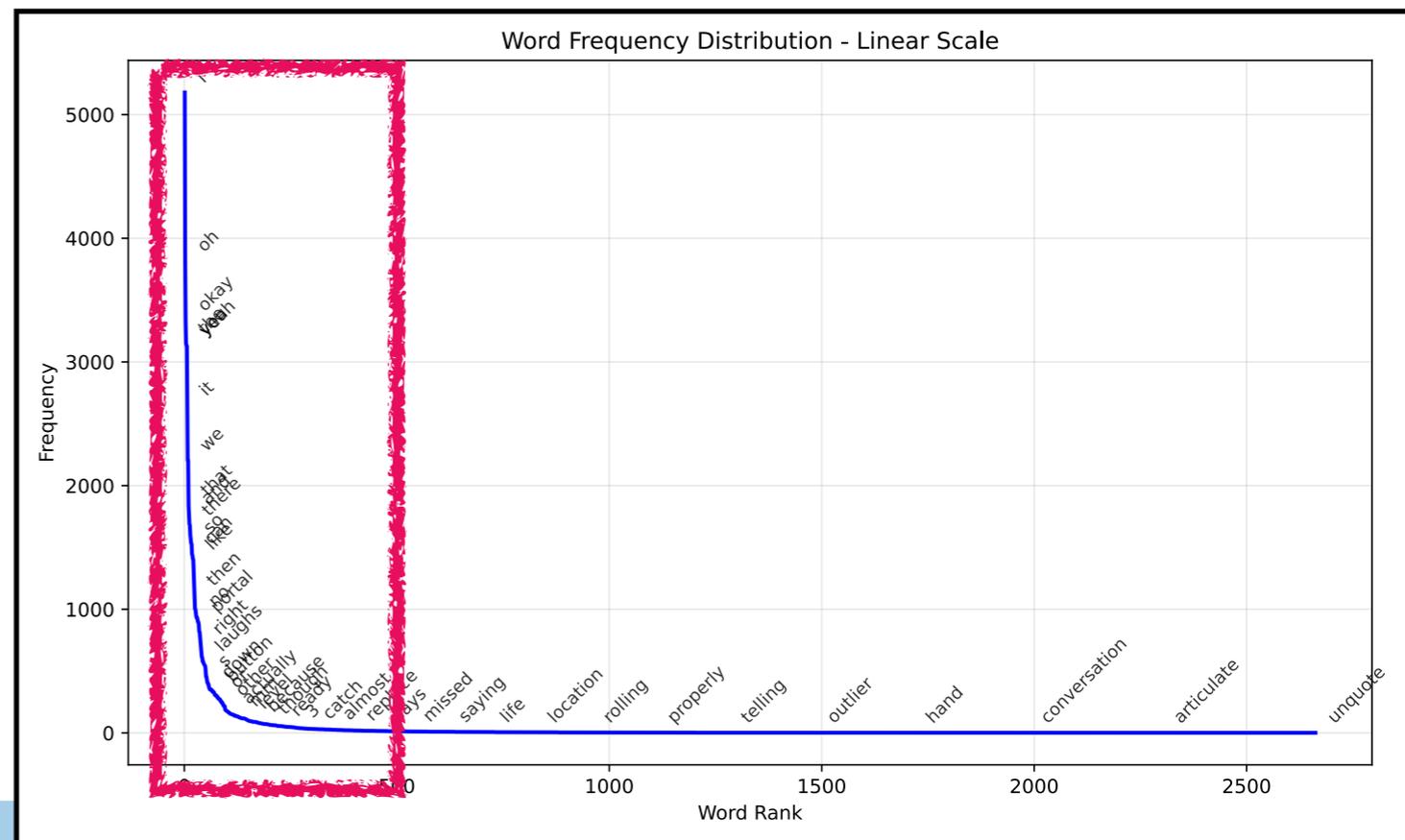
Masking Out Wordtypes



Operation: top-k sampling

- Identify the set of k tokens \mathcal{K} that have the highest probabilities under $p(X_i | x_1, \dots, x_{i-1})$
- Set the probabilities of all but these tokens to 0
- Renormalize by dividing remaining probabilities by

$$\sum_{x \in \mathcal{K}} p(X_i | x_1, \dots, x_{i-1})$$



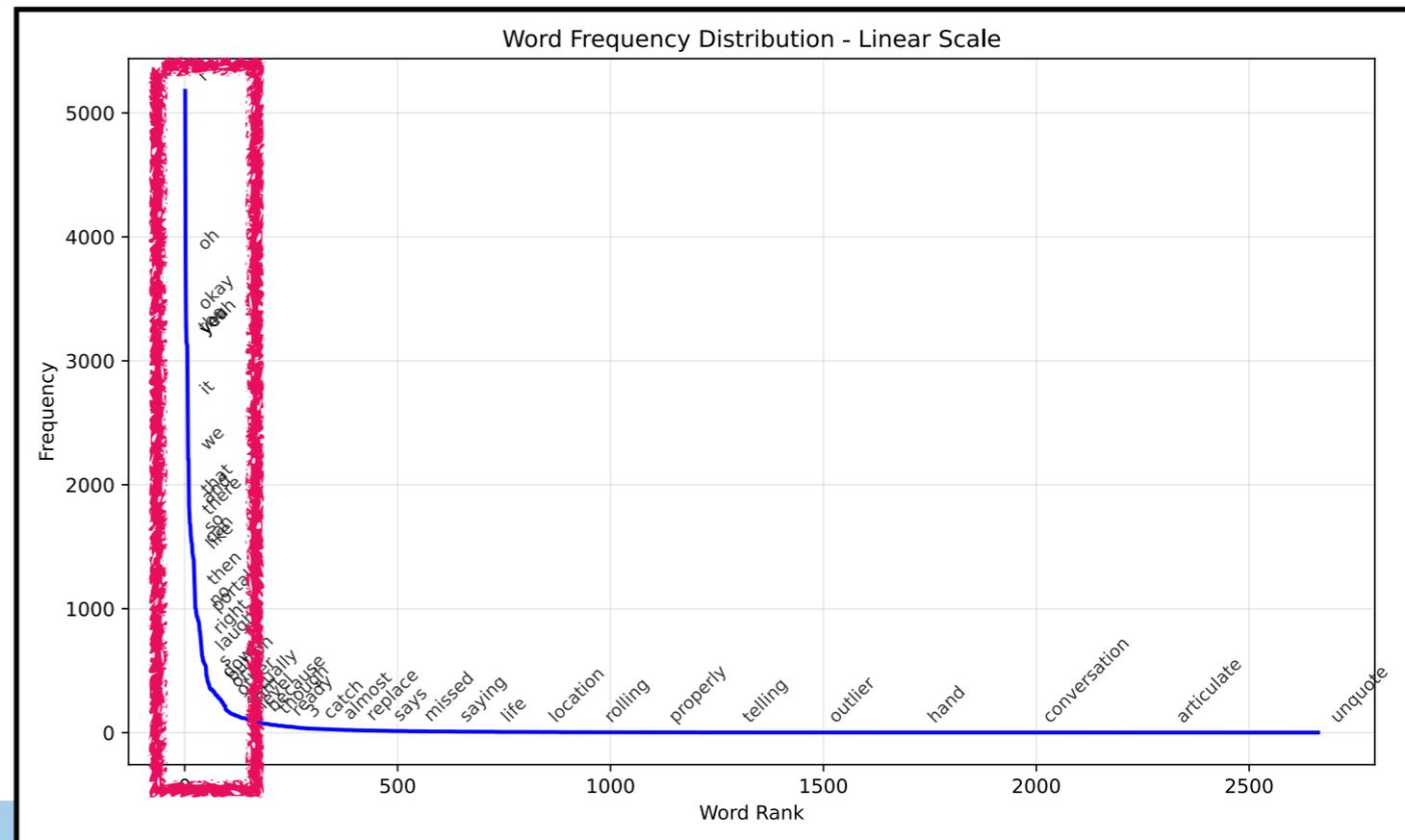
Masking Out Wordtypes



Operation: top-p (nucleus) sampling

- Identify the set of n tokens \mathcal{P} that have the highest probabilities under $p(X_i | x_1, \dots, x_{i-1})$ and their cumulative probability is p
- Set the probabilities of all but these tokens to 0
- Renormalize by dividing remaining probabilities by

$$\sum_{x \in \mathcal{P}} p(X_i | x_1, \dots, x_{i-1}) = p$$



Masking Out Wordtypes



Operation: constrained decoding

- For some tasks, we have additional information about what wordtypes can or cannot be next
- E.g., in code generation, I can't generate more) than I have (
- While modern LLMs can learn these patterns from data at scale, it can sometimes still be useful to constrain our output space

Masking Out Wordtypes



Operation: constrained decoding

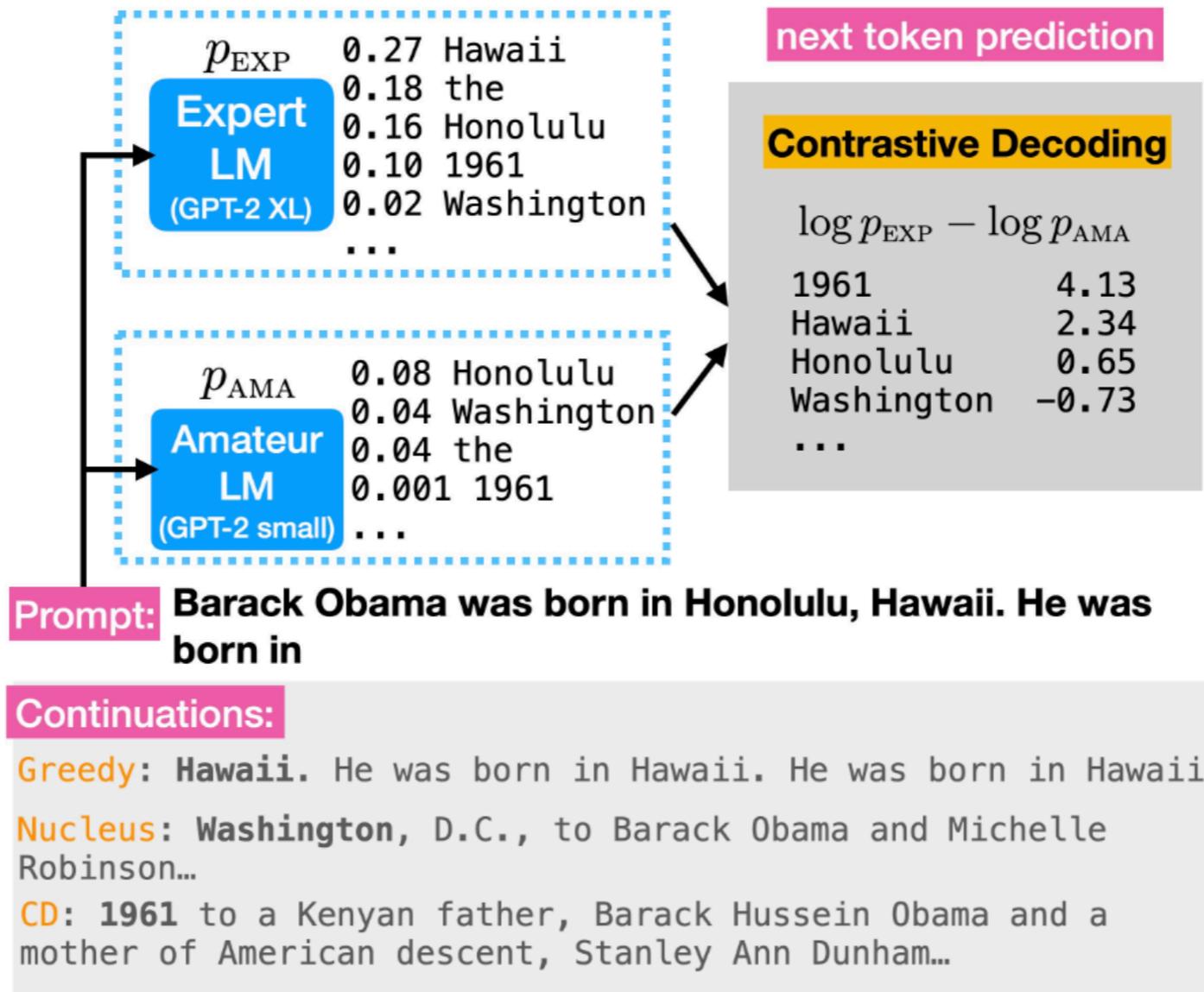
- For some tasks, we have additional information about what wordtypes can or cannot be next
- E.g., in code generation, I can't generate more) than I have (
- While modern LLMs can learn these patterns from data at scale, it can sometimes still be useful to constrain our output space
- Similar to before: given a set of possible continuations $\mathcal{C} \subseteq \mathcal{V}$ we will set the probabilities of all other tokens to 0, then renormalize using
$$\sum_{x \in \mathcal{C}} p(X_i | x_1, \dots, x_{i-1})$$

Contrastive Decoding



Operation: shift distribution away from
“amateur” model

$$\log p_{\text{EXP}}(\mathbf{x}_{\text{cont}} \mid \mathbf{x}_{\text{pre}}) - \log p_{\text{AMA}}(\mathbf{x}_{\text{cont}} \mid \mathbf{x}_{\text{pre}})$$



Inference-Time Optimizations: Speculative Decoding



- Observation: some tokens are easier to generate than others

What is the square root of 7?

The square root of **7** is **2.646**.

- Computing the distribution over tokens is slow for large models, and this must be done serially

$$x_i \sim p(\cdot \mid x_1, \dots, x_{i-1})$$

$$x_{i+1} \sim p(\cdot \mid x_1, \dots, x_{i-1}, x_i)$$

- Speculative execution: a system performs a task that may not be needed, to prevent a delay that would be incurred if the task was performed only after it was known that it was needed

- We need to be able to “suggest” tasks that might be needed in the future
- Here: we can approximate p with a faster model

Inference-Time Optimizations: Speculative Decoding



- First, (quickly) get a sample of the next token from a small model

$$x'_i \sim p'(\cdot \mid x_1, \dots, x_{i-1})$$

- Then, in parallel:

$$p(x'_i \mid x_1, \dots, x_{i-1})$$

Compute “actual” probability
of sampled token

$$x'_{i+1} \sim p(\cdot \mid x_1, \dots, x_{i-1}, x'_i)$$

Compute continuation, assuming
approximation was good

- After, we choose whether x'_i is “valid” or not

- If $p'(x'_i \mid x_1, \dots, x_{i-1}) \leq p(x'_i \mid x_1, \dots, x_{i-1})$

(i.e., probability according to approximation is less than actual probability), we keep it as valid

- Otherwise, we keep it as valid with probability:

$$\frac{p(x'_i \mid x_1, \dots, x_{i-1})}{p'(x'_i \mid x_1, \dots, x_{i-1})}$$

Inference-Time Optimizations: Speculative Decoding



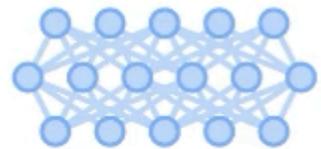
- If x'_i is deemed not valid, then we sample from a new distribution:
$$x''_i \sim \text{norm max}(0, p(\cdot | x_1, \dots, x_{i-1}) - p'(\cdot | x_1, \dots, x_{i-1}))$$

“Residual” probability on tokens that
the “actual” model assigned higher probability
to than the approximation
- This process is exactly equivalent to sampling directly from $p(\cdot | x_1, \dots, x_{i-1})$, but (fast) look-ahead generation can be parallelized with verification
- Original speculative decoding paper extends this to sampling multi-token suffixes with the approximation model
 - Multi-token suffixes are easy to verify in a single forward pass with the “actual” model

Inference-Time Optimizations: Speculative Decoding

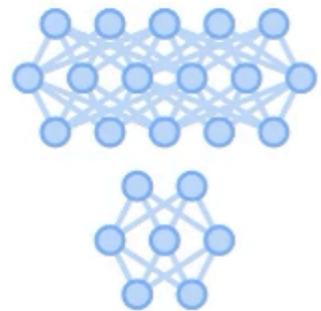


WITHOUT SPECULATIVE DECODING



My favorite thing about fall

WITH SPECULATIVE DECODING

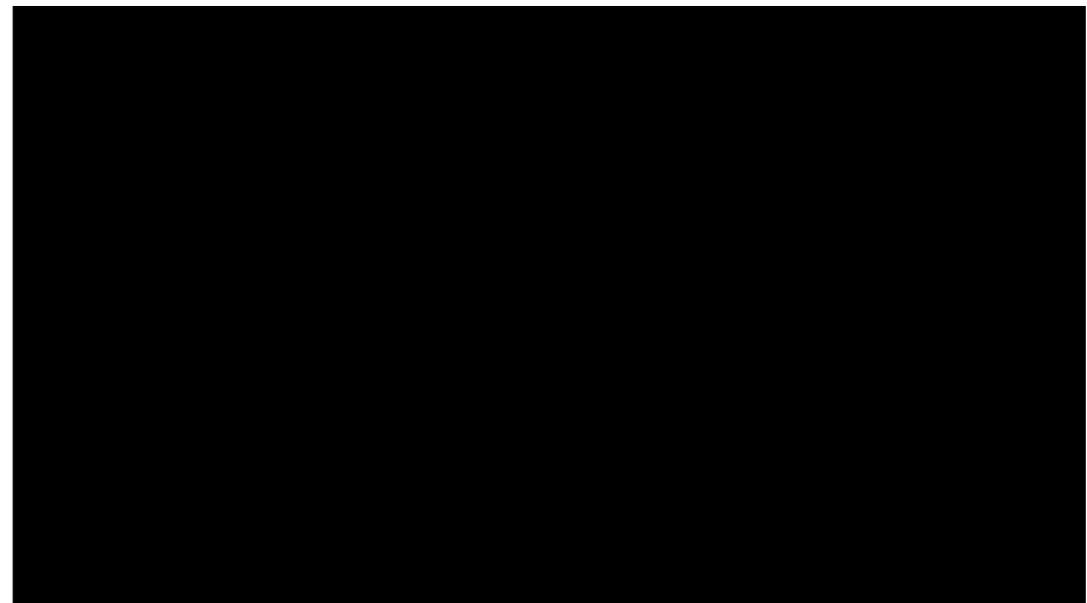
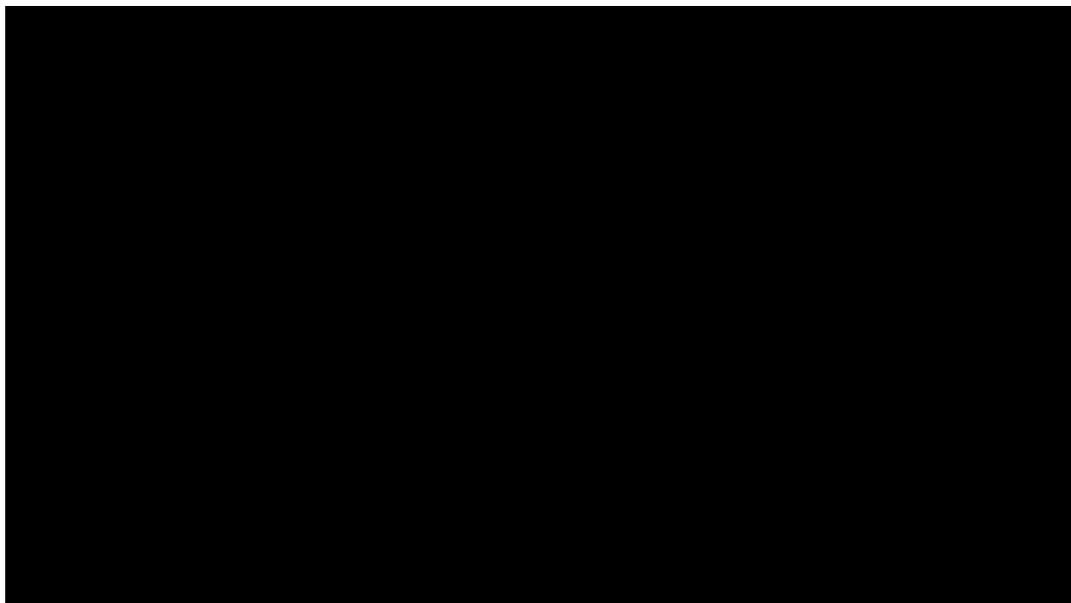


My favorite thing about fall

Inference-Time Optimization: KV Caching



- When a token is first seen, compute and store its keys and values in a cache
- Every time we process a new (sampled) token as input, retrieved the stored key/value from previous tokens, instead of recomputing them



- One consideration: you can only do this if you keep a fixed prefix of tokens

Inference-Time Optimization: Quantization



- **Main principle:** use lower-precision representations of network parameters during inference
- Reduces the space required to store the model during inference
- If your model has 65B parameters...
 - float32 (single-precision) → 260 GB
 - float16 (half-precision) → 130 GB
 - Usually doesn't influence performance significantly!
 - 1-byte precision → 65 GB
 - 1-bit precision → 8.1 GB

Inference with Modern LLMs



- Today's LLMs aren't simply distributions over texts, but distributions over text conditioned on a *prompt*
- But we can still use the same sampling methods as before

$$p(\bar{Y} | x) \in \Delta^{\mathcal{V}^+}$$

- People recommend different parameters for different LLMs and different tasks
- Inference engines (vLLM, sglang, LightLLM, etc.) implement hardware-optimized inference algorithms for open-weight models

Use Case	Temperature	Top_p	Description
Code Generation	0.2	0.1	Generates code that adheres to established patterns and conventions. Output is more deterministic and focused. Useful for generating syntactically correct code.
Creative Writing	0.7	0.8	Generates creative and diverse text for storytelling. Output is more exploratory and less constrained by patterns.
Chatbot Responses	0.5	0.5	Generates conversational responses that balance coherence and diversity. Output is more natural and engaging.
Code Comment Generation	0.3	0.2	Generates code comments that are more likely to be concise and relevant. Output is more deterministic and adheres to conventions.
Data Analysis Scripting	0.2	0.1	Generates data analysis scripts that are more likely to be correct and efficient. Output is more deterministic and focused.
Exploratory Code Writing	0.6	0.7	Generates code that explores alternative solutions and creative approaches. Output is less constrained by established patterns.

ruv, 2023, ChatGPT API recommendations