## Natural Language Processing



Compositional Semantics

Truth-Conditional Semantics

## Truth-Conditional Semantics

- Linguistic expressions:
- "Bob sings"
- Logical translations:
- sings(bob)

- Could be p_1218(e_397)
- Denotation:
- [[bob]] = some specific person (in some context)
- [[sings(bob)]] = ???
- Types on translations:
- bob:e
- sings(bob):t


## Truth-Conditional Semantics

- Proper names:
- Refer directly to some entity in the world
- Bob:bob [[bob]]w $\rightarrow$ ???
- Sentences:
- Are either true or false (given how the world actually is)
- Bob sings : sings(bob)

- So what about verbs (and verb phrases)?
- sings must combine with bob to produce sings(bob)
- The $\lambda$-calculus is a notation for functions whose arguments are not yet filled.
- sings : $\lambda x$.sings( $x$ )
- This is a predicate - a function which takes an entity (type e) and produces a truth value (type t). We can write its type as $\mathrm{e} \rightarrow \mathrm{t}$.
- Adjectives?


## Compositional Semantics

- So now we have meanings for the words
- How do we know how to combine words?
- Associate a combination rule with each grammar rule:
- $S: \beta(\alpha) \rightarrow N P: \alpha$ VP : $\beta$ (function application)
- VP $: \lambda x . \alpha(x) \wedge \beta(x) \rightarrow V P: \alpha$ and $: \varnothing$ VP: $\beta$ (intersection)
- Example:



## Denotation

- What do we do with logical translations?
- Translation language (logical form) has fewer ambiguities
- Can check truth value against a database
- Denotation ("evaluation") calculated using the database
- Or the opposite: assert truth and modify a database, either explicitly or implicitly eg prove a consequence from asserted axioms
- Questions: check whether a statement in a corpus entails the (question, answer) pair:
- "Bob sings and dances" $\rightarrow$ "Who sings?" + "Bob"
- Chain together facts and use them for comprehension


## Other Cases

- Transitive verbs:
- likes: $\lambda x . \lambda y . l i k e s(y, x)$
- Two-place predicates of type $\mathrm{e} \rightarrow(\mathrm{e} \rightarrow \mathrm{t})$.
- likes Amy : $\lambda$ y.likes(y,Amy) is just like a one-place predicate.
- Quantifiers:
- What does "Everyone" mean here?
- Everyone : $\lambda \mathrm{f} . \forall \mathrm{x} . \mathrm{f}(\mathrm{x})$
- Mostly works, but some problems
- Have to change our NP/VP rule.
- Won't work for "Amy likes everyone."
- "Everyone likes someone."
- This gets tricky quickly!



## Indefinites

- First try
- "Bob ate a waffle" : ate(bob,waffle)
- "Amy ate a waffle" : ate(amy,waffle)
- Can't be right!
- ヨx:waffle(x) ^ ate(bob,x)
- What does the translation
of "a" have to be?
- What about "the"?
- What about "every"?



## Grounding

- Grounding
- So why does the translation likes : $\lambda x . \lambda y$.likes $(y, x)$ have anything to do with actual liking?
- It doesn't (unless the denotation model says so)
- Sometimes that's enough: wire up bought to the appropriate entry in a database
- Meaning postulates
- Insist, e.g $\forall x, y$.likes $(y, x) \rightarrow$ knows $(y, x)$
- This gets into lexical semantics issues
- Statistical / neural version?


## Tense and Events

- In general, you don't get far with verbs as predicates
- Better to have event variables e
- "Alice danced" : danced(alice)
- ヨe:dance(e) $\wedge$ agent(e,alice) $\wedge($ time $(e)<$ now $)$
- Event variables let you talk about non-trivial tense / aspect structures
- "Alice had been dancing when Bob sneezed"
- ヨe, e': dance(e) $\wedge$ agent(e,alice) $\wedge$

```
sneeze(e') ^ agent(e',bob) ^
(start(e) < start(e') ^ end(e) = end(e')) ^
(time(e') < now)
```

- Minimal recursion semantics, cf "object oriented" thinking


## Adverbs

- What about adverbs?
- "Bob sings terribly"
- terribly(sings(bob))?
- (terribly(sings))(bob)?
- ヨe present(e) ^ type(e, singing) $\wedge$ agent(e,bob)

$\wedge$ manner(e, terrible) ?
- Gets complex quickly...


## Propositional Attitudes

- "Bob thinks that I am a gummi bear"
- thinks(bob, gummi(me)) ?
- thinks(bob, "I am a gummi bear") ?
- thinks(bob, ^gummi(me)) ?
- Usual solution involves intensions (^X) which are, roughly, the set of possible worlds (or conditions) in which X is true
- Hard to deal with computationally
- Modeling other agents' models, etc
- Can come up in even simple dialog scenarios, e.g., if you want to talk about what your bill claims you bought vs. what you actually bought


## Trickier Stuff

- Non-Intersective Adjectives
- green ball: $\lambda x$.[green(x) $\wedge$ ball(x)]
- fake diamond : $\lambda x$. $[$ fake $(\mathrm{x}) \wedge$ diamond $(\mathrm{x})]$ ? $\longrightarrow \lambda x$.[fake(diamond $(\mathrm{x}))$
- Generalized Quantifiers
- the: $\lambda \mathrm{f}$.[unique-member(f)]
- all : $\lambda \mathrm{f} . \lambda \mathrm{g}[\forall \mathrm{x} . \mathrm{f}(\mathrm{x}) \rightarrow \mathrm{g}(\mathrm{x})]$
- most?
- Could do with more general second order predicates, too (why worse?)
- the(cat, meows), all(cat, meows)
- Generics
- "Cats like naps"
- "The players scored a goal"
- Pronouns (and bound anaphora)
- "If you have a dime, put it in the meter."
- ... the list goes on and on!


## Scope Ambiguities

- Quantifier scope
- "All majors take a data science class"
- "Someone took each of the electives"
- "Everyone didn't hand in their exam"
- Deciding between readings
- Multiple ways to work this out
- Make it syntactic (movement)
- Make it lexical (type-shifting)


## Logical Form Translation

## Mapping to LF: Zettlemoyer \& Collins 05/07

## The task:

```
    Input: List one way flights to Prague.
    Output: \lambdax.flight(x)^ one_way(x)^ to(x,PRG)
```


## Challenging learning problem:

- Derivations (or parses) are not annotated
- Approach: [Zettlemoyer \& Collins 2005]
- Learn a lexicon and parameters for a weighted Combinatory Categorial Grammar (CCG)


## Background

- Combinatory Categorial Grammar (CCG)
- Weighted CCGs
- Learning lexical entries: GENLEX


## CCG Parsing

- Combinatory Categorial Grammar
- Fully (mono-) lexicalized grammar
- Categories encode argument sequences
- Very closely related to the lambda calculus
- Can have spurious ambiguities (why?)

$$
\begin{aligned}
& \text { John } \vdash \mathrm{NP}: \text { john }^{\prime} \\
& \text { shares } \vdash \mathrm{NP}: \text { shares }^{\prime} \\
& \text { buys } \vdash(\mathrm{S} \backslash \mathrm{NP}) / \mathrm{NP}: \lambda x . \lambda y . \text { buys' }^{\prime} x y \\
& \text { sleeps } \vdash \mathrm{S} \backslash \mathrm{NP}: \lambda x . \text { sleeps }^{\prime} x \\
& \text { well } \vdash(\mathrm{S} \backslash \mathrm{NP}) \backslash(\mathrm{S} \backslash \mathrm{NP}): \lambda f . \lambda x . \text { well }^{\prime}(f x)
\end{aligned}
$$

## CCG Lexicon

| Words | Category |
| :---: | :---: |
| flights | $\mathrm{N}: \lambda x . f l i g h t(x)$ |
| to | $(N \backslash N) / N P: \lambda x . \lambda f . \lambda y \cdot f(x) \wedge t o(y, x)$ |
| Prague | $N P: P R G$ |
| New York city | $N P: N Y C$ |
| $\ldots$ | $\cdots$ |

## Parsing Rules (Combinators)

## Application



Composition

- $X / Y: f \quad Y / Z: g \quad=>/ Z: \lambda x . f(g(x))$
- $Y \backslash Z$ : $f \quad X \backslash Y$ : $g=>X \backslash Z: \lambda x . f(g(x))$

Additional rules:

- Type Raising
- Crossed Composition


## CCG Parsing

| Show me | flights | to | Prague |
| :---: | :---: | :---: | :---: |
| S/N | N | ( $\mathrm{N} \backslash \mathrm{N}$ ) /NP | NP |
| $\lambda f . f$ | $\lambda \mathrm{x} . \mathrm{flight}^{\text {(x) }}$ | $\lambda y . \lambda f . \lambda x . f(y) \wedge t o(x, y)$ | PRG |
|  |  | $\mathbf{N} \backslash \mathbf{N}$ <br> $\lambda f . \lambda x . f(x) \wedge t o(x, P R G)$ |  |
|  |  |  |  |
|  |  | N |  |
| $\lambda x . f l i g h t(x) \wedge t \bigcirc(x, P R G)$ |  |  |  |
| S |  |  |  |
| $\lambda \mathrm{x} . \mathrm{flight}(\mathrm{x}) \wedge$ to (x, PRG) |  |  |  |

## Weighted CCG

Given a log-linear model with a CCG lexicon $\Lambda$, a feature vector $f$, and weights $w$.

- The best parse is:

Where we consider all possible parses $y$ for the sentence $x$ given the lexicon $\Lambda$.

## Lexical Generation

## Input Training Example

```
Sentence:
Show me flights to Prague.
Logic Form: \(\lambda x . f l i g h t(x) \wedge\) to (x,PRG)
```

Output Lexicon

| Words | Category |
| :---: | :---: |
| Show me | $\mathrm{S} / \mathrm{N}: \lambda \mathrm{f} \cdot \mathrm{f}$ |
| flights | $\mathrm{N}: \lambda x \cdot f l i g h t(x)$ |
| to | $(\mathrm{N} \backslash \mathrm{N}) / \mathrm{NP}: \lambda x \cdot \lambda f \cdot \lambda y \cdot f(x) \wedge$ to $(y, x)$ |
| Prague | $\mathrm{NP}: P R G$ |
| $\ldots$ | $\ldots$ |

## GENLEX: Substrings X Categories

Input Training Example

| Sentence: | Show me flights to Prague. |
| :--- | :--- |
| Logic Form: | $\lambda x$. flight $(x) \wedge$ to $(x, P R G)$ |
| Output Lexicon |  |

All possible substrings:

```
```

Show

```
```

Show

```
```

Show
me
me
me
flights
flights
flights
show me
show me
show me
Show me flights
Show me flights
Show me flights
Show me flights to

```
```

    Show me flights to
    ```
```

    Show me flights to
    ```
```

    Show me
    Categories created by rules that trigger on the logical form:

NP : PRG
X
$N: \lambda_{x} . f l i g h t(x)$
(S $\backslash N P$ ) /NP : $\lambda_{x} \cdot \lambda y \cdot t o(y, x)$
$(N \backslash N) / N P: \lambda_{y} \cdot \lambda f \cdot \lambda_{x}$.

Inputs: Training set $\left\{\left(x_{i}, z_{i}\right) \mid i=1 \ldots n\right\}$ of sentences and logical forms. Initial lexicon $\Lambda$. Initial parameters $w$. Number of iterations $T$.
Training: For $t=1 \ldots T, i=1 \ldots n$ :
Step 1: Check Correctness

- Let
- If $L\left(y^{*}\right)=z_{i}$, go to the next example

Step 2: Lexical Generation

- Set
- Let
- Define $\lambda_{i}$ to be the lexical entries in $y^{\wedge}$
- Set lexicon to $\Lambda=\Lambda \cup \lambda_{i}$

Step 3: Update Parameters

- Let
- If
- Set

Output: Lexicon $\Lambda$ and parameters $w$.

